



Dynamics of Nonlinear Interactions between Electron Temperature Gradient Mode and Ion-scale Fluctuations in Linear Magnetized Plasmas

**Chanho Moon^{1,2}, Toshiro Kaneko², Rikizo Hatakeyama²,
Tatsuya Kobayashi¹, Kimitaka Itoh¹**

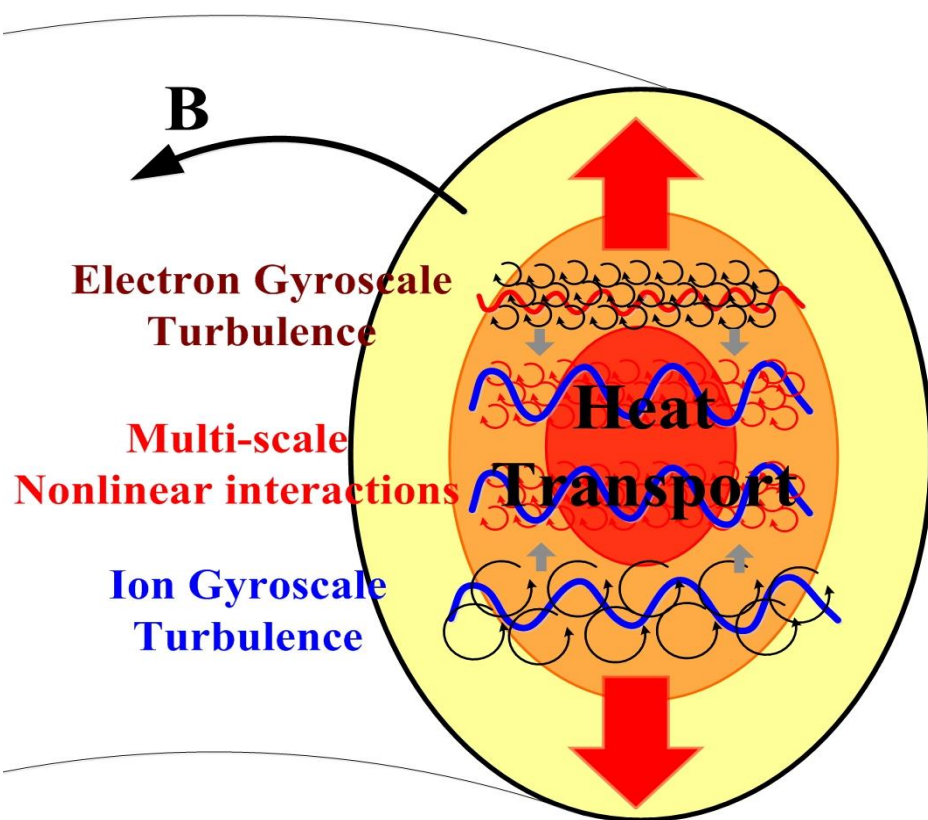
¹*National Institute for Fusion Science, 322-6 Oroshi-cho, Toki-shi, 509-5292, Japan*

²*Department of Electronic Engineering, Tohoku University, Sendai 980-8579, Japan*

E-mail : *moon.chanho@LHD.nifs.ac.jp*

- 1. Background and Purpose**
- 2. Experimental Apparatus**
- 3. Experimental Results**
- 4. Summary**

Background and Purpose



- Open problems on ETG mode
- Excitation mechanism
- Suppression mechanism

- 1) W. Horton, Rev. Mod. Phys. **71** (1999) 735.
- 2) F. Brochard et al., Phys. Plasmas **12** (2005) 062104.
- 3) V. Sokolov et al., Phys. Rev. Lett. **89** (2002) 095001.
- 4) S. K. Mattoo et al., Phys. Rev. Lett. **108** (2012) 255007.

Anomalous heat transport — ion scale —

Gradient Driven Instability

- Drift wave (DW) mode¹⁾
- Flute mode²⁾
- Ion temperature gradient (ITG) mode³⁾

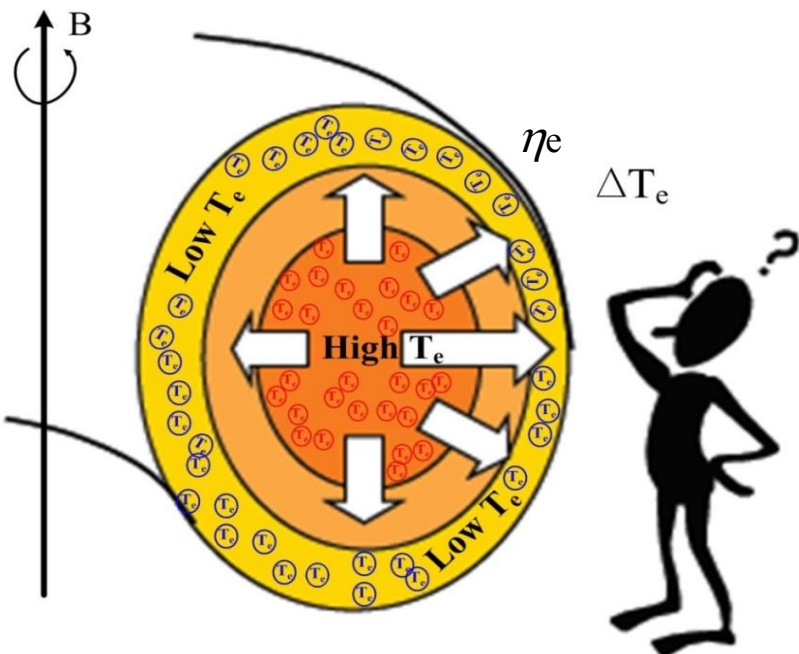
Anomalous electron heat transport

Electron Temperature Gradient (ETG) Mode⁴⁾

electron heat transport	\sim	ion heat transport
	$(\chi_e \sim \chi_i)$	

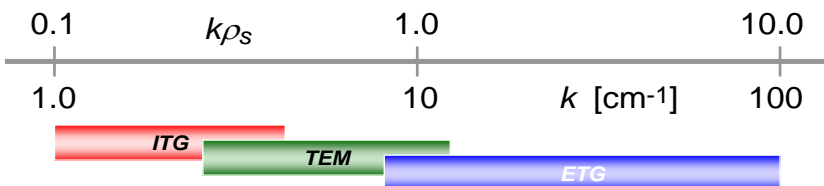
Produce and control the ETG to **understand the mechanism of excitation and multi-scale interaction of the ETG mode**

Research of ETG mode



ETG mode:

- **Electrostatic mode (low β)**
- **Electron diamagnetic direction**
- $k_{\perp} \rho_e \leq 1 < k_{\perp} \rho_i, \Omega_i < \omega \ll \Omega_e$



Wavelength scales of Fluctuations

Theory

✓ Excitation

- Y. C. Lee et al., Phys. Fluids **30**, 1331 (1987).
- W. Horton and B. G. Hong, Phys. Fluids **31**, 2971 (1988).
- Y. Idomura et al., Phys. Plasmas **7**, 2456 (2000).
- W. Dorland et al., Phys. Rev. Lett. **85**, 5579 (2000).
- S. -I. Itoh and K. Itoh, Plasma Phys. Control. Fusion **43**, 1055 (2001).
- F. Jenko, J. Plasma Fusion Res. Ser. **6**, 11 (2004).

Multi-Scale Interactions

✓ Suppression

- Z. Gao et al., Phys. Plasmas **11**, 3053 (2004).
- M. Romanelli et al., Phys. Plasmas **11**, 3845 (2004).

Experiment


✓ Excitation

- E. Mazzucato et al., Phys. Rev. Lett. **101**, 075001 (2008).
→ **Observation**
- X. Wei et al., Phys. Plasmas **17**, 042108 (2010).
→ **Identification**
- X. R. Fu et al., Phys. Rev. Lett. **19**, 032303 (2012).
→ **High β**

✓ Suppression

- D. R. Smith et al., Phys. Rev. Lett. **102**, 225005 (2009).
→ **Large $E \times B$ Shear**
- H. Y. Yuh et al., Phys. Rev. Lett. **106**, 055003 (2011).
→ **Magnetic Shear**

∇ -Driven Instability / Turbulence

	Excitation 'Bare' Instability	Multi-Scale Interaction	Suppression
Ion-scale $\sim \rho_i$	<ul style="list-style-type: none"> • Drift wave ~ 1960 • Geometrical ~ 1980 (∇B, ...) • Trapped particle • ITG mode ~ 1990 	<ul style="list-style-type: none"> • Geodesic acoustic mode (Conway, Nagashima) • Zonal flow (Fujisawa, ...) • Streamer (Yamada, ...) <p>※Causal relations</p> <p>“Multi-scale Renormalized Turbulence”</p>	<ul style="list-style-type: none"> • $E \times B$ flow shear • linear or nonlinear
Electron-scale $\sim \rho_e$	<p>※Experi.</p> <ul style="list-style-type: none"> ✓ <u>ETG mode</u> • Observation (E. Mazzucato) ~ 2008 • Identification (X. Wei) ~ 2010 • High β (X. R. Fu) ~ 2012 		<ul style="list-style-type: none"> • Large $E \times B$ shear (D. R. Smith) • Magnetic Shear (H. Y. Yuh) • Density Gradient (Y. Ren)
Electron-scale $\sim \rho_e$	<p>※Theories</p> <ul style="list-style-type: none"> ✓ <u>ETG mode</u> (Horton, Dorland, Jenko,) ~ 1990 	<ul style="list-style-type: none"> • Elongated toroidal (cascade, Jenko) • Nonlinear ion-scale DW (radially elongated, Itoh, Jenko) • Streamer (Idomura) • Zonal flow (?) feeble (Diamond) 	<ul style="list-style-type: none"> • $E \times B$ shear (Z. Gao)

National Spherical Torus Experiment (NSTX)

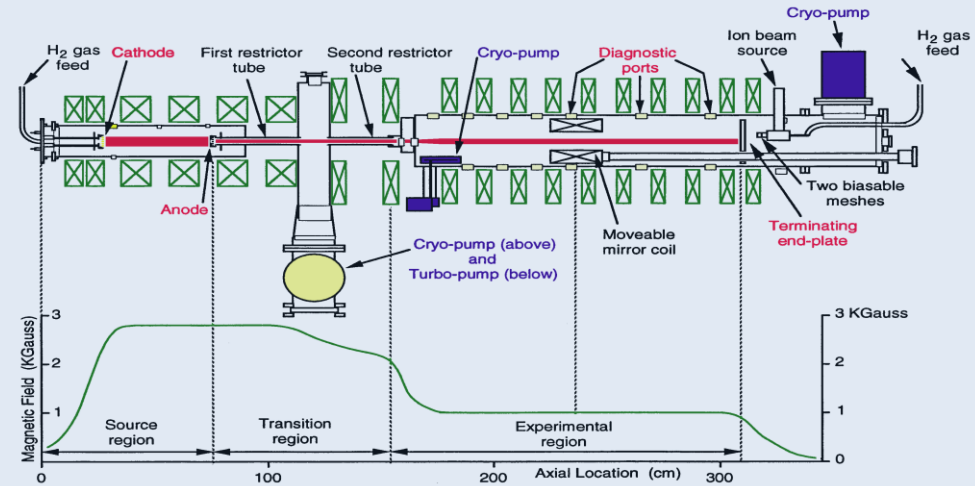


Fluctuations : $\omega/2\pi \sim 1$ MHz
 $T_e = \sim 2$ keV, $n_e = \sim 4 \times 10^{19} \text{ m}^{-3}$

- **Troidal Device**
- **Difficult to Control ETG**
- **Changing Plasma Parameters**

Columbia Linear Machine (CLM)

Columbia Linear Machine



Fluctuations : $\omega/2\pi \sim 2$ MHz
 $T_e = 5-15$ eV, $n_e = \sim 2 \times 10^{15} \text{ m}^{-3}$

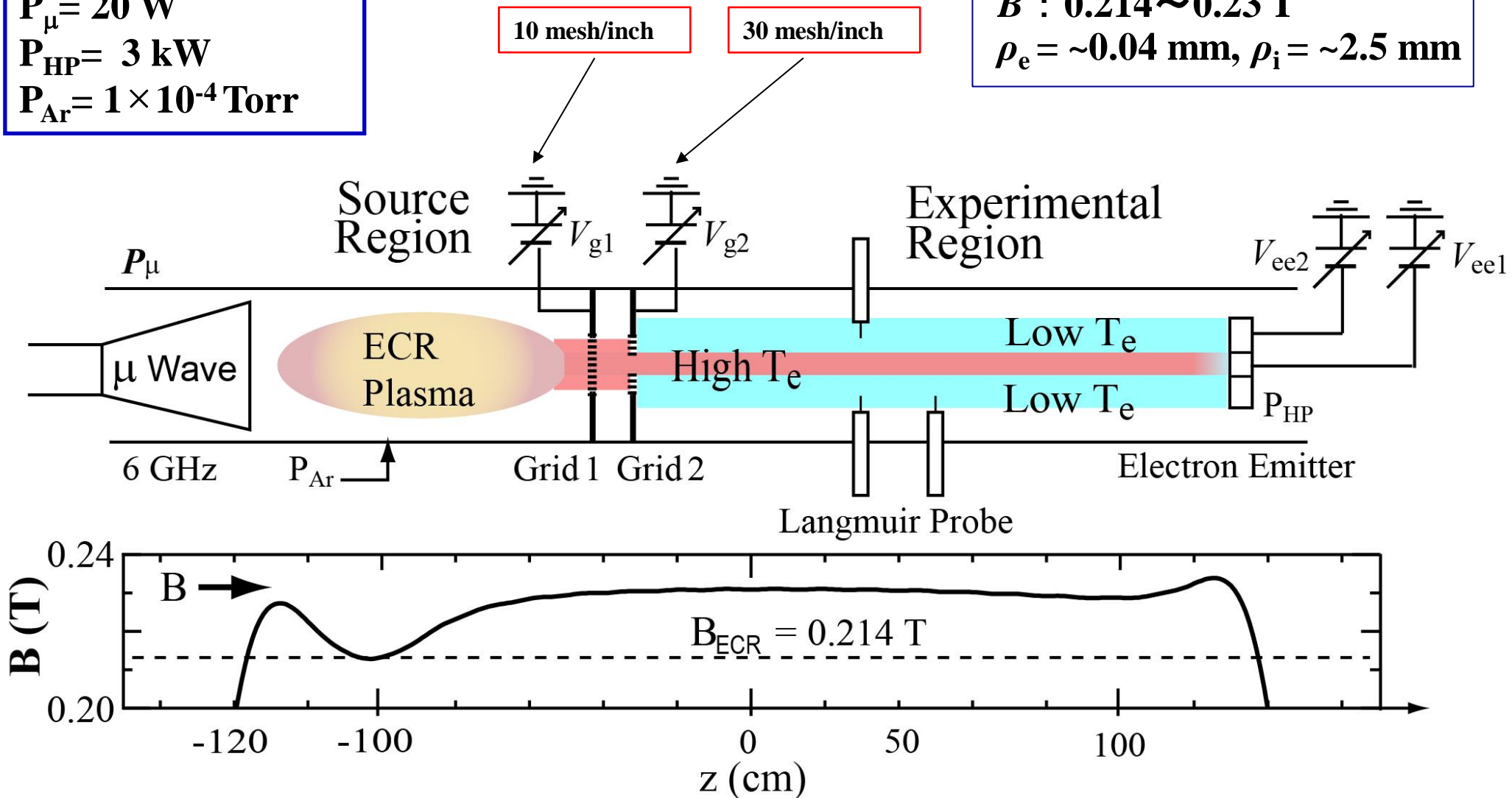
- **Linear Device**
- **Using the Electron Beam**
- **Forming the Density Gradient**

Experimental Apparatus

7

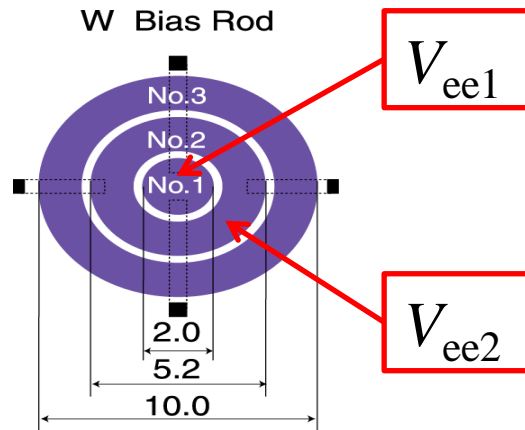
$P_{\mu} = 20 \text{ W}$
 $P_{\text{HP}} = 3 \text{ kW}$
 $P_{\text{Ar}} = 1 \times 10^{-4} \text{ Torr}$

$B : 0.214 \sim 0.23 \text{ T}$
 $\rho_e = \sim 0.04 \text{ mm}, \rho_i = \sim 2.5 \text{ mm}$



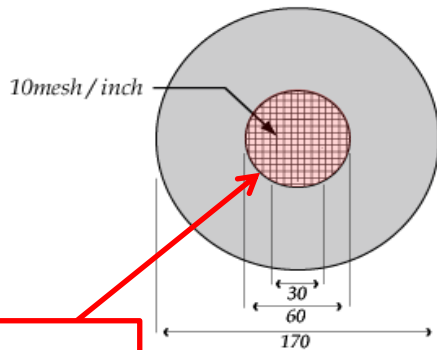
Q_T Upgrade Machine at Tohoku University

Electron emitter (W hot plate)

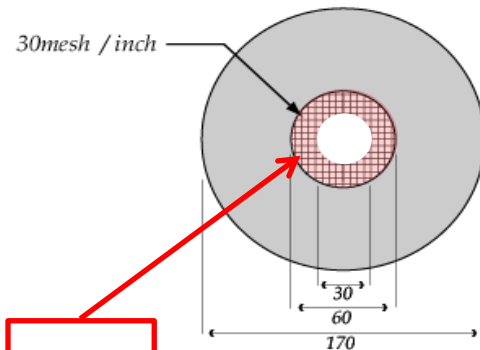


Configuration of mesh grids

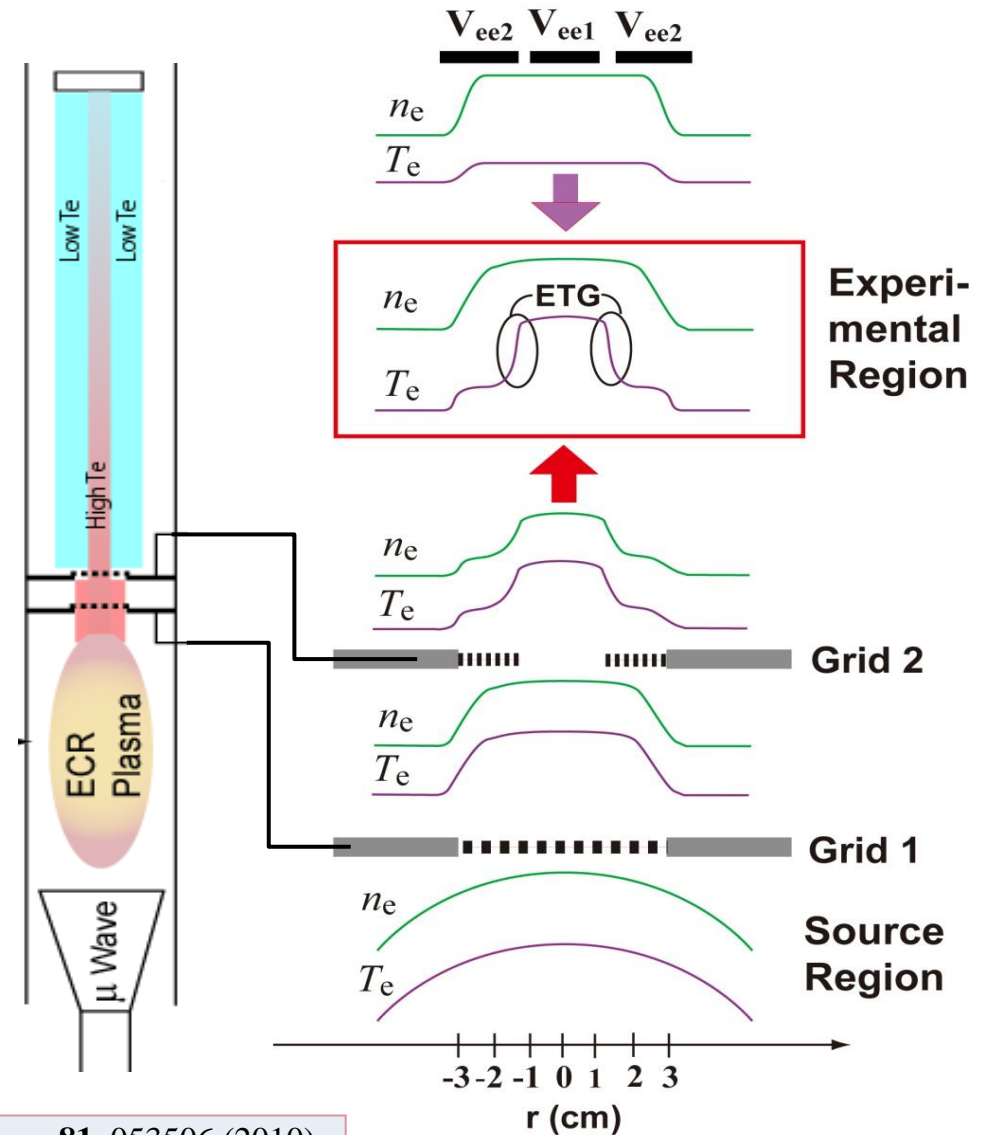
Grid 1



Grid 2



Electron emitter

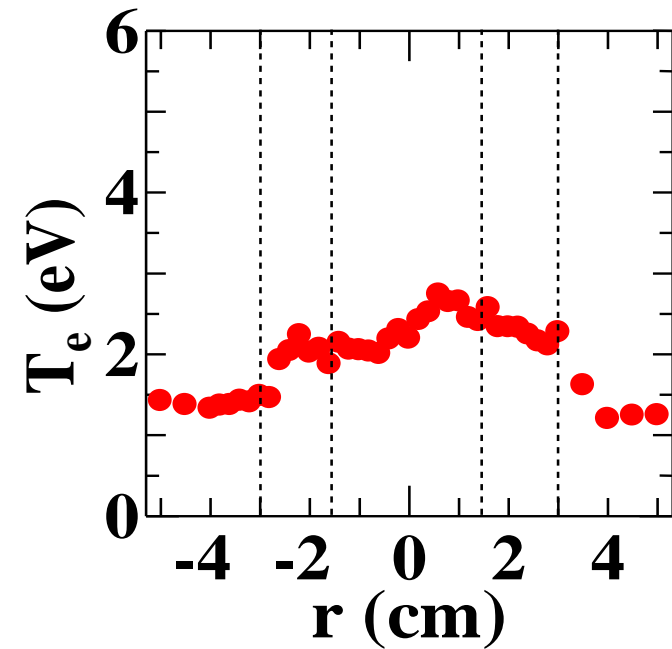


C. Moon, T. Kaneko, S. Tamura, and R. Hatakeyama, Rev. Sci. Instrum. **81**, 053506 (2010).

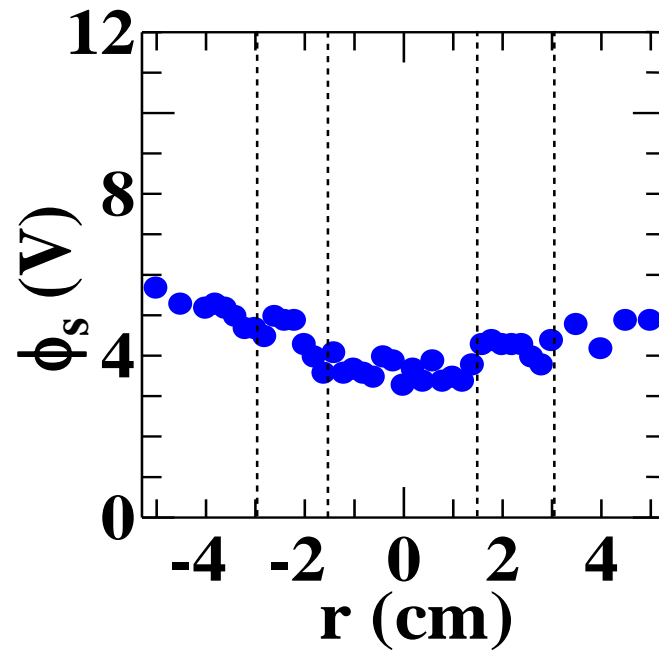
Control of the electron density and temperature profiles from the source to experimental regions by using the mesh grids.

$$P_{\mu} = 60 \text{ W}, P_{\text{HP}} = 3 \text{ kW}, P_{\text{Ar}} = 1 \times 10^{-4} \text{ Torr}$$
$$V_{g1} = 0 \text{ V}, V_{g2} = 0 \text{ V}, V_{ee1} = 0 \text{ V}, V_{ee2} = 0 \text{ V}$$

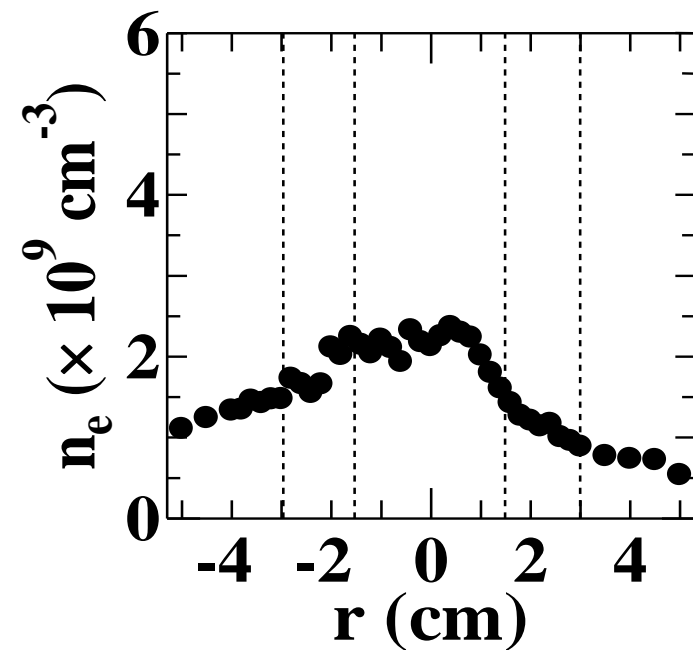
Electron Temperature



Space Potential



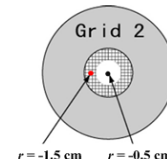
Electron Density



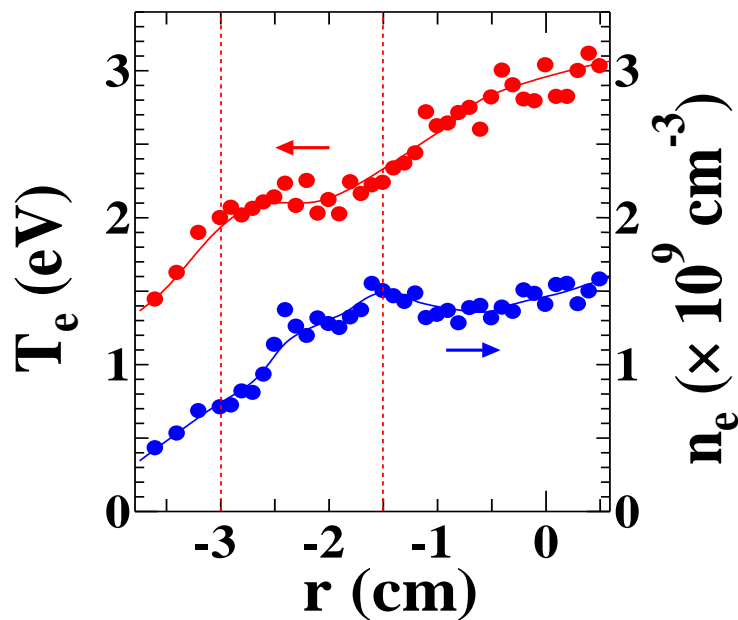
Radial Profiles of a Typical Plasma Parameters

Formation and Control of ETG

$$P_{\mu} = 20 \text{ W}, V_{ee1} = -4 \text{ V}, V_{ee2} = -1.5 \text{ V}, V_{g1} = -10 \text{ V}$$

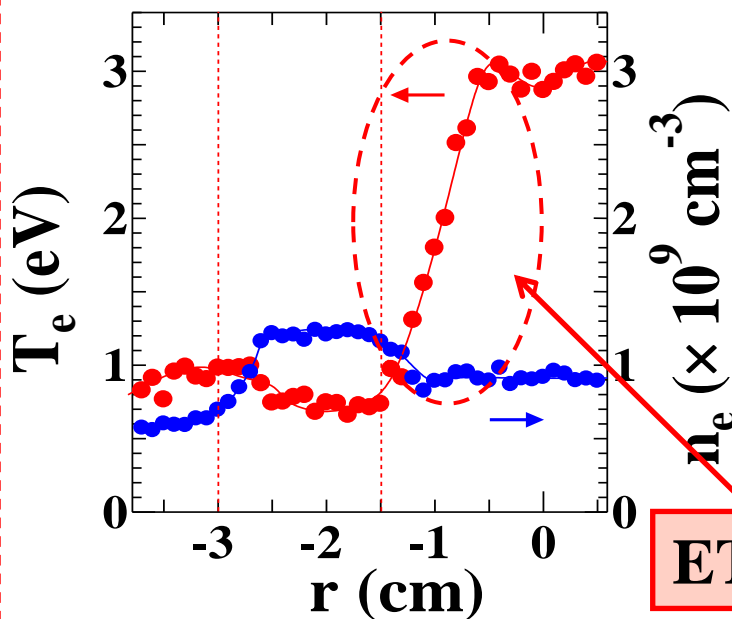


$r = -1.5 \text{ cm}$ $r = -0.5 \text{ cm}$

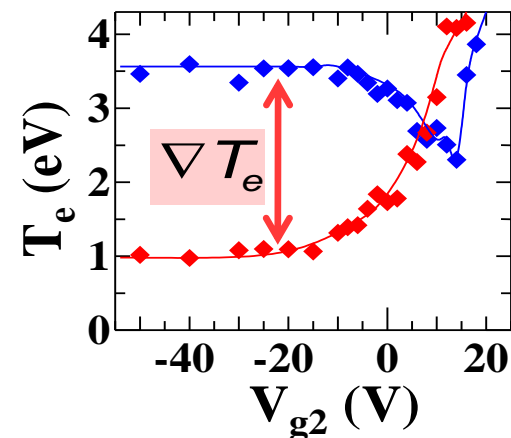


$$V_{g2} = 3 \text{ V}$$

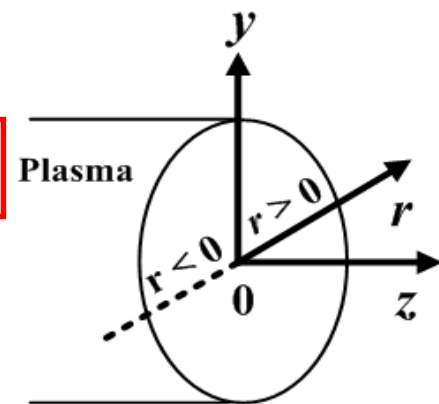
$r = -1.5 \text{ cm}$ $r = -0.5 \text{ cm}$



$$V_{g2} = -30 \text{ V}$$



ETG

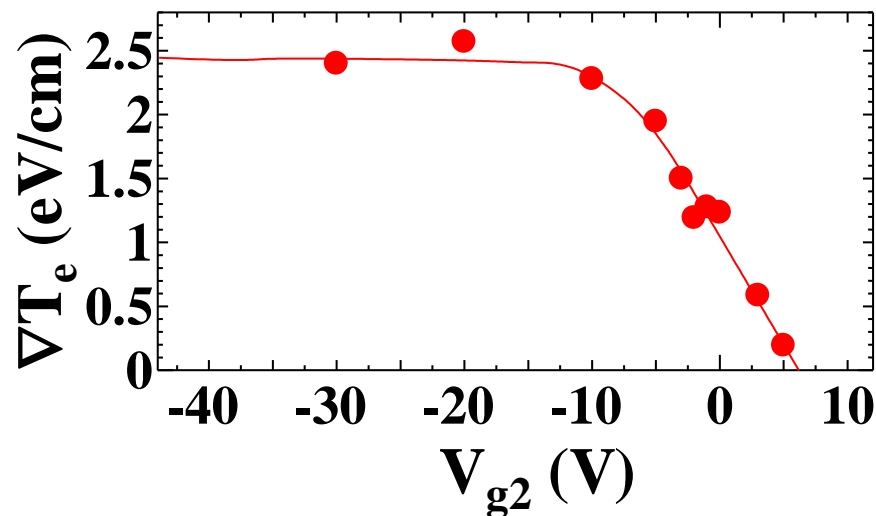


ETG can be generated easily by controlling the grid bias voltages V_{g2} .

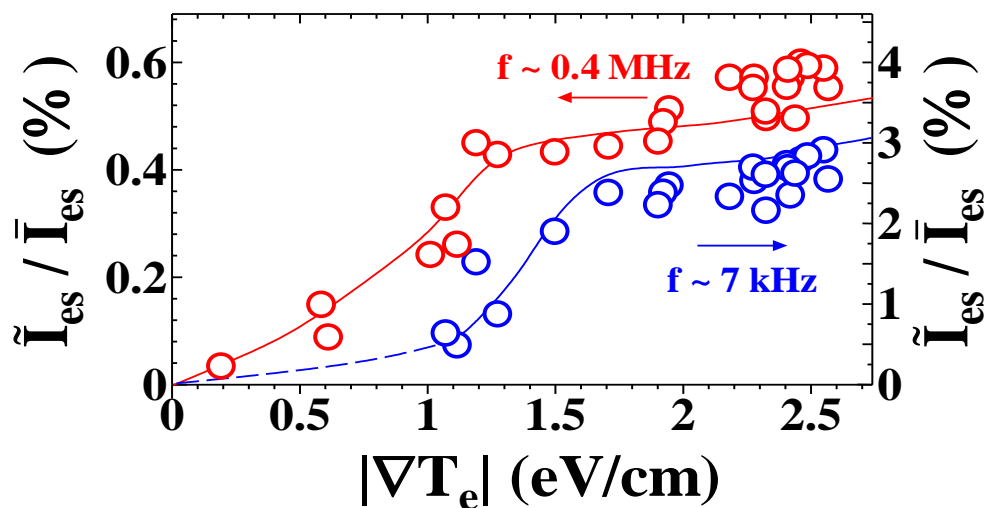
Effect of ETG on Fluctuations

$P_{\mu} = 20 \text{ W}$, $V_{ee1} = -4 \text{ V}$
 $V_{ee2} = -1.5 \text{ V}$, $V_{g1} = -10 \text{ V}$
 $r = -1.5 \text{ cm}$

ETG (∇T_e)



Normalized Amp.



high and low frequency

A high-frequency fluctuation ($\sim 0.4 \text{ MHz}$) is excited in situations where large ETG is formed (ETG mode).

Linear Dispersion Relations

The perturbed electron density of the linearized Vlasov equation:

$$\tau + (k_{\perp} \lambda_{De})^2 + b \left(1 + \frac{1}{2\lambda_e^2} \right) - \frac{1}{2\lambda_e^2} + b \frac{\omega_{Te}^*}{\omega} + \frac{\omega_{Te}^*}{4\lambda_e^2 \omega} (1 + b) = 0,$$

where $\tau = \frac{T_e}{T_i}$, $k_{\perp} = k_y$, $\lambda_e = \frac{\omega}{k_{\parallel} v_e}$, $b = \frac{(k_{\perp} \rho_e)^2}{2}$, $\omega_{Te}^* = \frac{k_{\perp} T_e}{eBL_{Te}}$.

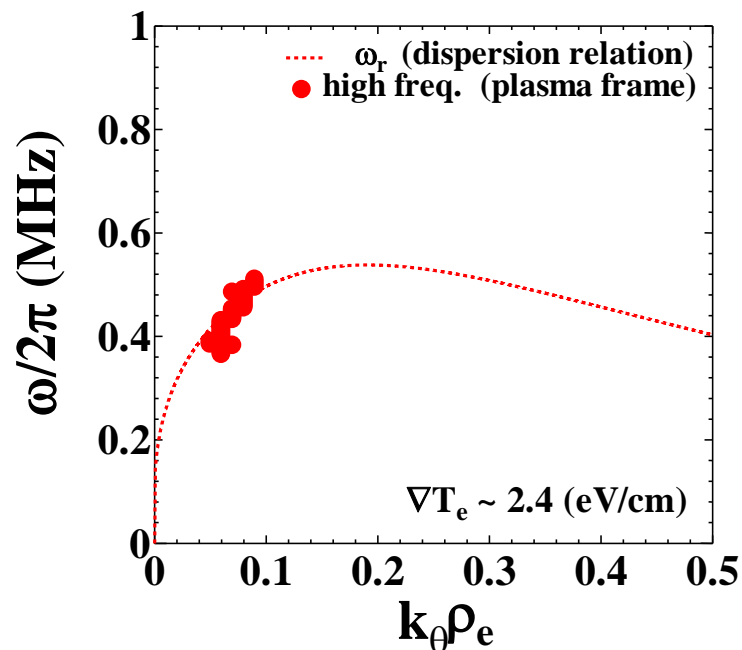
[Phys. Fluids **30**, 1331 (1987), Phys. Plasmas **17**, 042108 (2010)]

The typical experimental plasma parameters

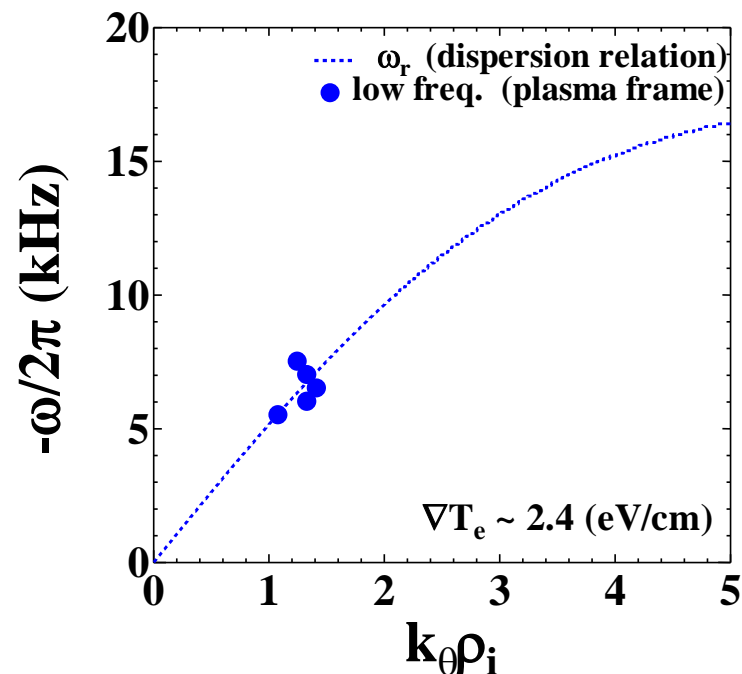
$$T_{e0} = 3 \text{ eV}, T_i = 0.3 \text{ eV}, n_e = 1 \times 10^9 \text{ cm}^{-3},$$

$$\lambda_{De} = 0.039 \text{ cm}, B = 2300 \text{ G}, L_{Te} = 1.2 \text{ cm},$$

$$k_{\parallel} = 0.06 \text{ cm}^{-1}, \rho_e = 0.004 \text{ cm}, \rho_i = 0.25 \text{ cm}.$$



ETG mode (~ 0.4MHz)



DW mode (~7 kHz)

The high and low frequency of fluctuations are consistent with the theoretical estimation from the linear dispersion relation of ETG and DW

Bicoherence: the degree of nonlinear coupling between the three waves (the value in the range from 0 to 1)

The bicoherence is defined as

$$b_{xyz}^2(f_1, f_2) = \frac{\left| \langle \mathbf{B}_{xyz}(f_1, f_2) \rangle \right|^2}{\left\langle \left| \mathbf{X}(f_1 + f_2) \right|^2 \right\rangle \left\langle \left| \mathbf{Y}(f_1) \mathbf{Z}(f_2) \right|^2 \right\rangle}$$

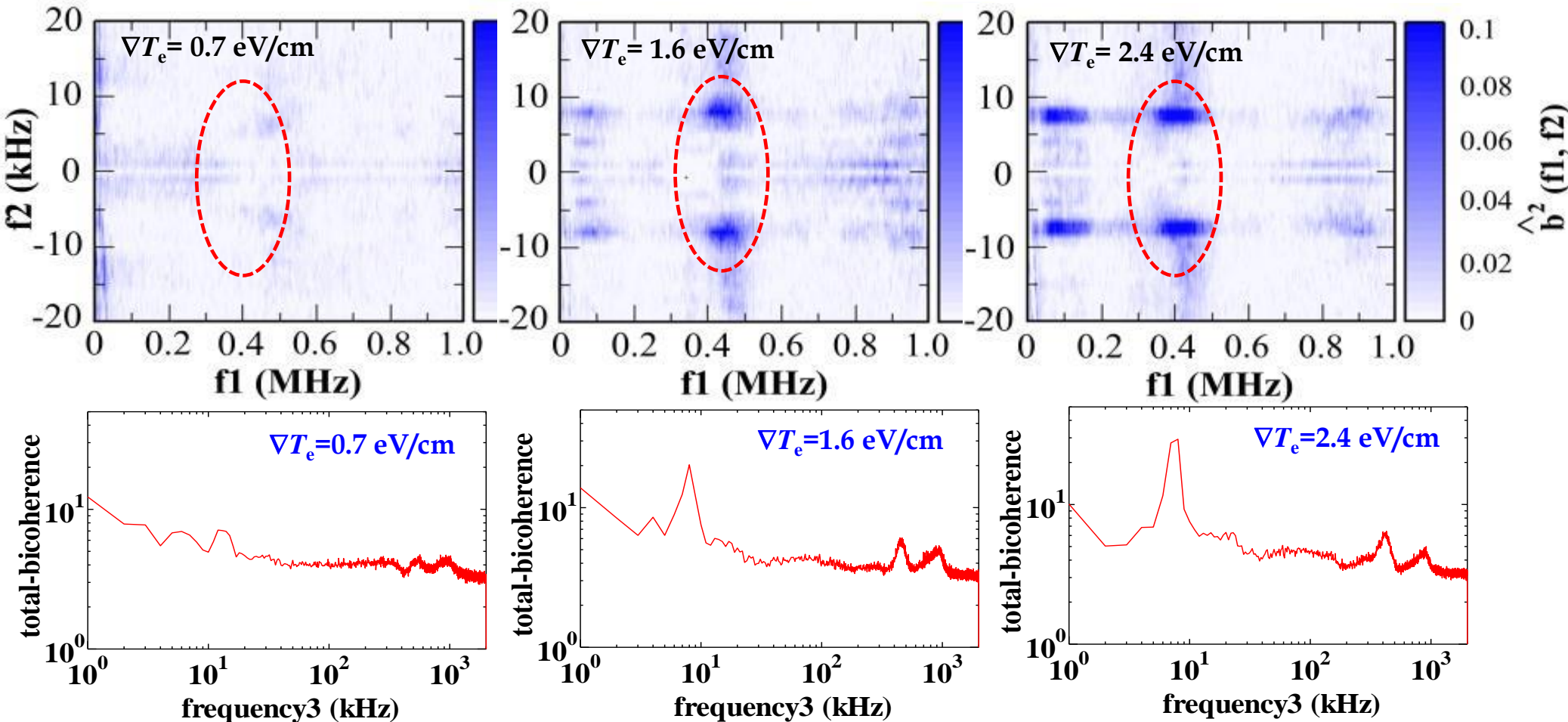
$\langle \rangle$: Averaged ensembles

• The variance of the bicoherence is $d b^2(f_1 + f_2) \leq 1/N \sim 0.0014$.

The bispectral analysis can clarify the three-wave nonlinear interactions quantitatively.

Squared Bicoherence

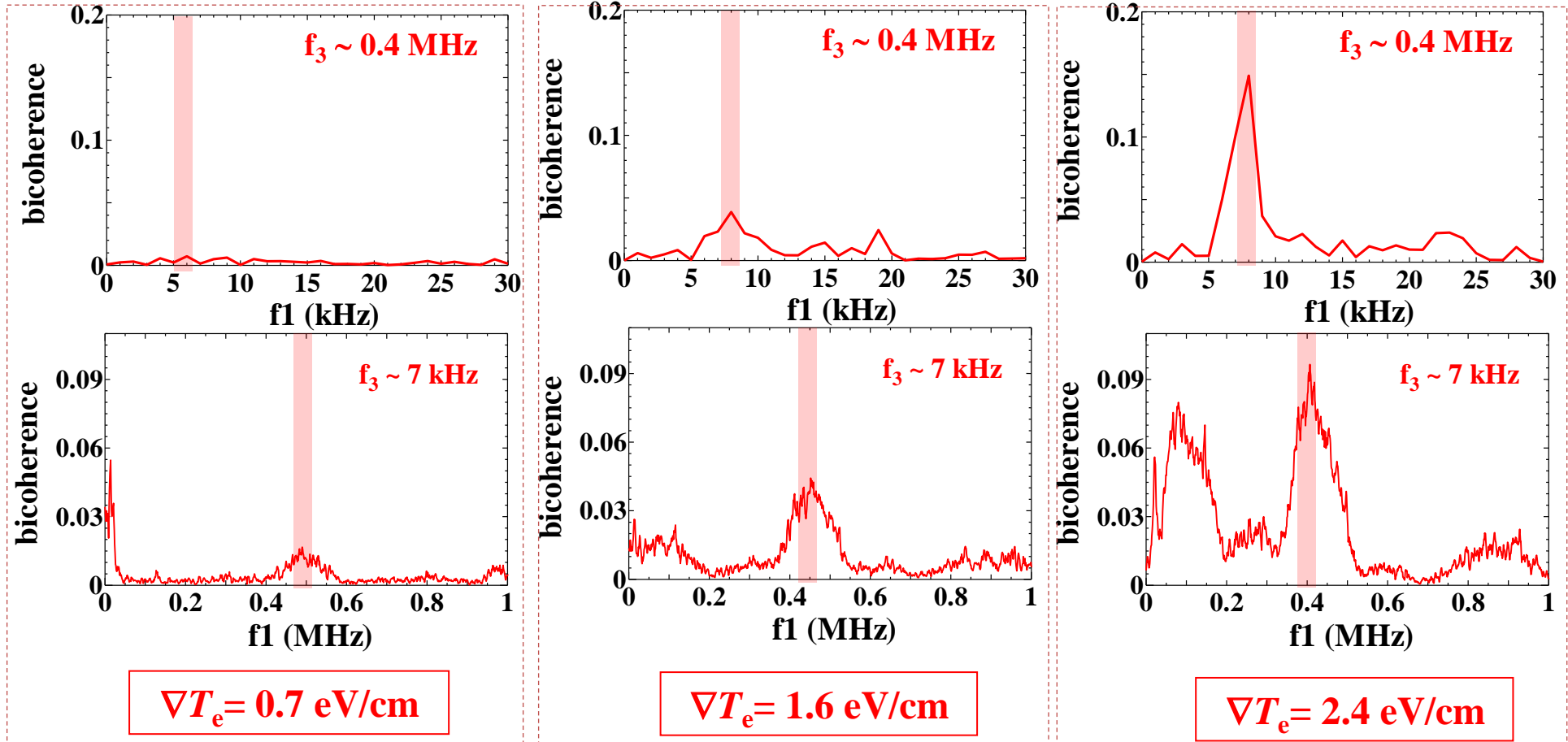
$$P_{\mu} = 20 \text{ W}, V_{g1} = -10 \text{ V}, V_{ee1} = -4.0 \text{ V}, \\ V_{ee2} = -1.5 \text{ V}, r = -1.5 \text{ cm}$$



The nonlinear coupling between the ETG mode and drift wave (DW) mode become stronger as the magnitude of ETG is increased.

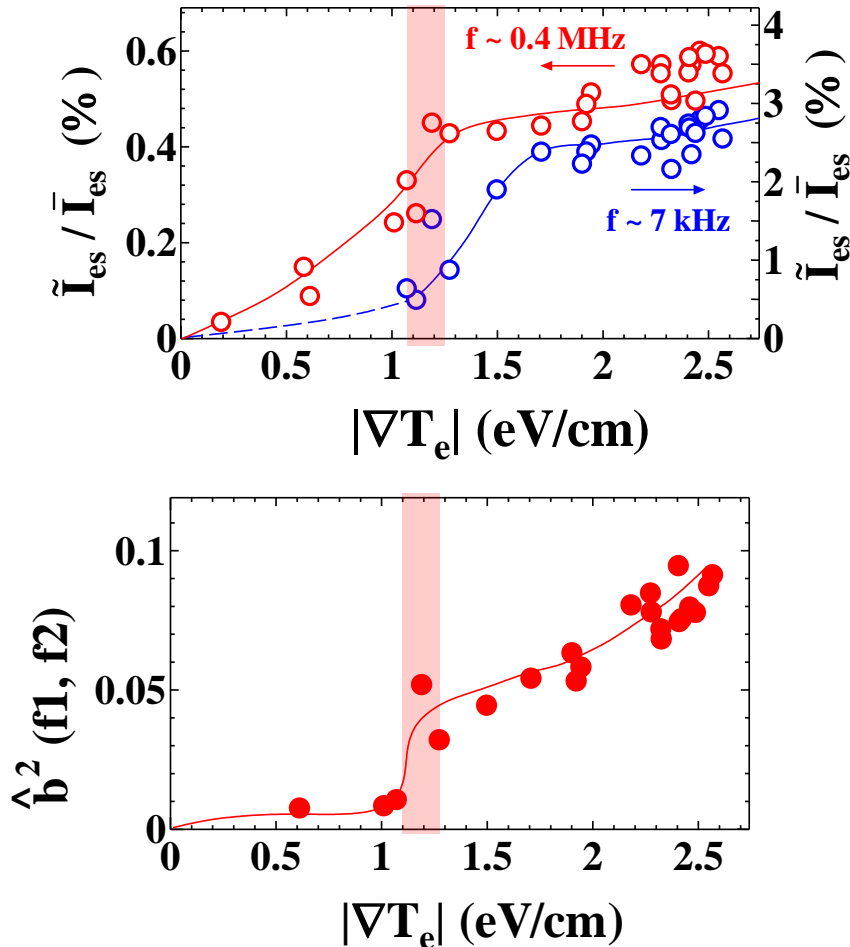
ETG (~ 0.4 MHz) & DW (~ 7 kHz) modes

$$P_{\mu} = 20 \text{ W}, V_{g1} = -10 \text{ V}, V_{ee1} = -4.0 \text{ V}, \\ V_{ee2} = -1.5 \text{ V}, r = -1.5 \text{ cm}$$



When the magnitude of ETG is increased, the slice of bicoherence between ETG mode and drift wave mode has a noticeable peak.

$$P_{\mu} = 20 \text{ W}, V_{g1} = -10 \text{ V}, V_{ee1} = -4 \text{ V}, V_{ee2} = -1.5 \text{ V}, r = -1.5 \text{ cm}$$



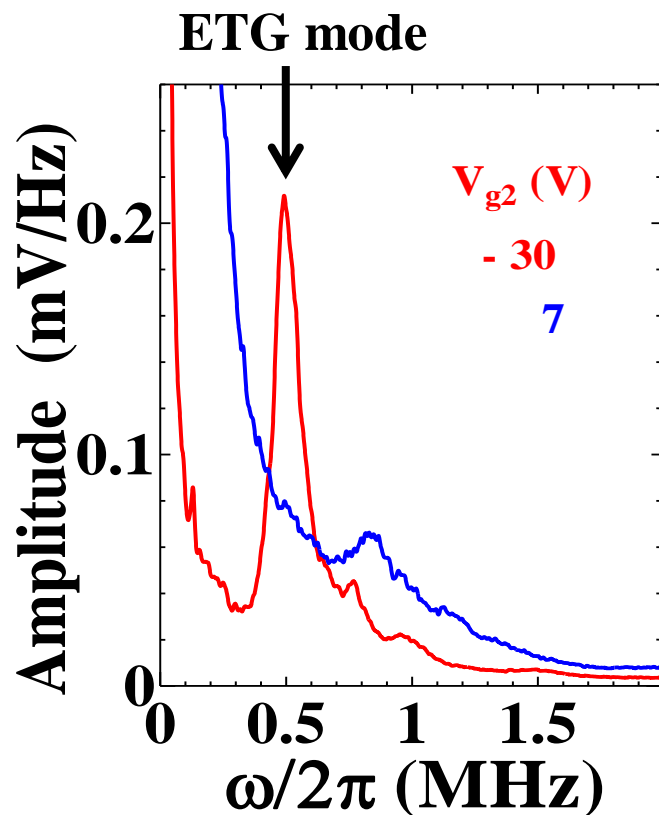
※ High-frequency fluctuations (ETG mode) versus low-frequency fluctuations (Drift wave mode).

C. Moon, T. Kaneko, and R. Hatakeyama,
Phys. Rev. Lett. **111**, 115001 (2013).

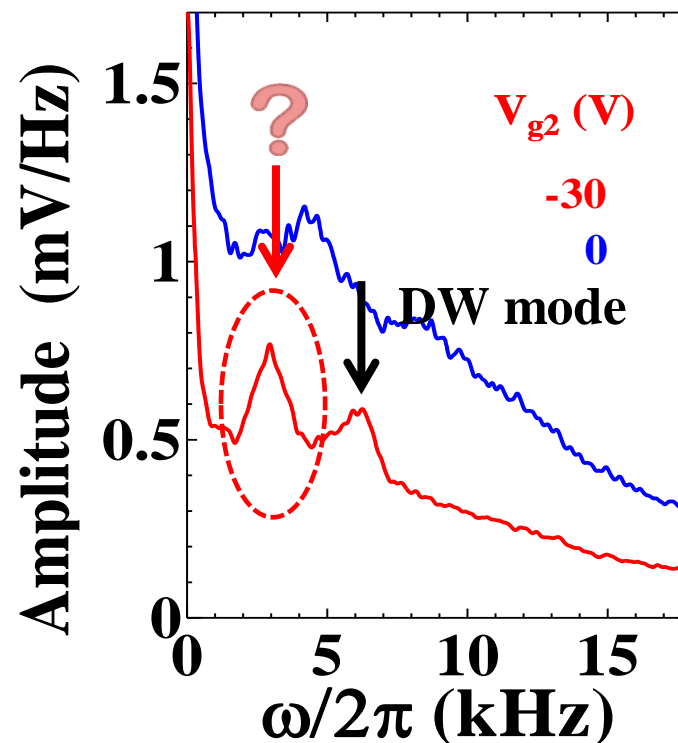
The energy of the ETG mode is transferred to the drift wave mode through the nonlinear interaction for $\nabla T_e \geq 1.2$ eV/cm.

Effect of ETG on Fluctuations

$$P_{\mu} = 20 \text{ W}, V_{ee1} = -4 \text{ V}, V_{ee2} = -1.5 \text{ V}, V_{g1} = -10 \text{ V}, r = -0.9 \text{ cm}$$



High-Frequency

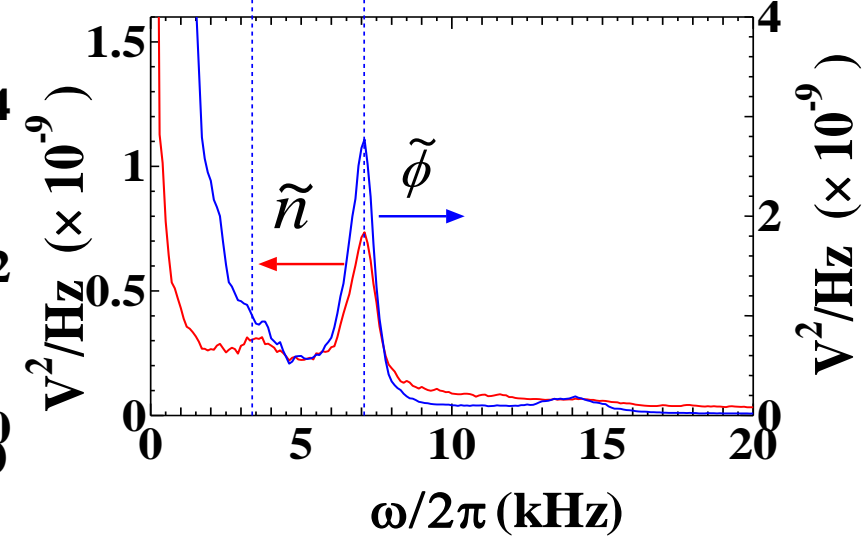
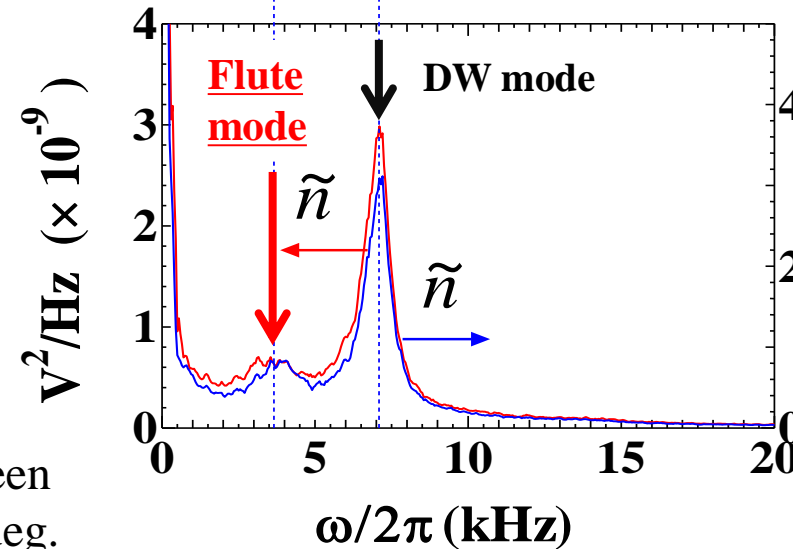
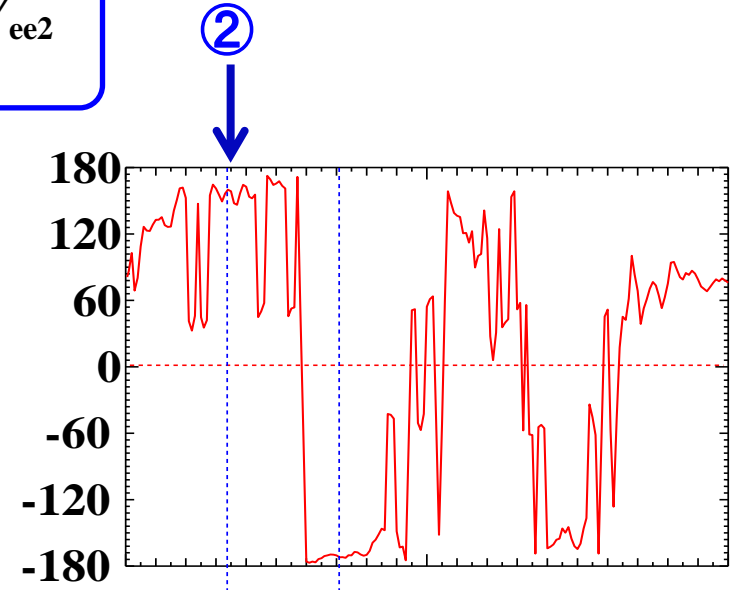
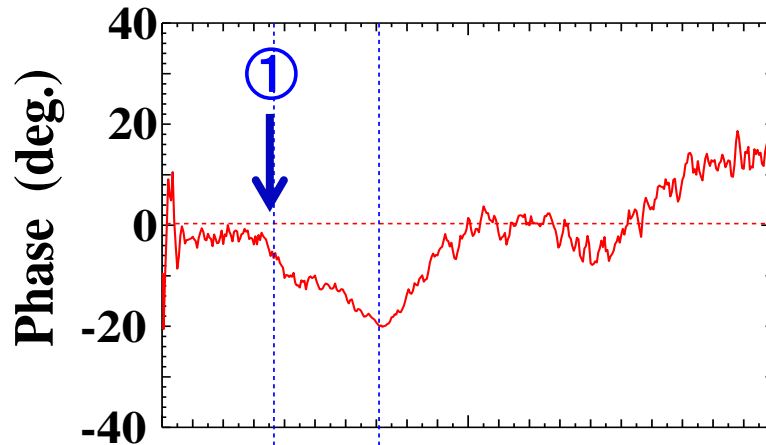
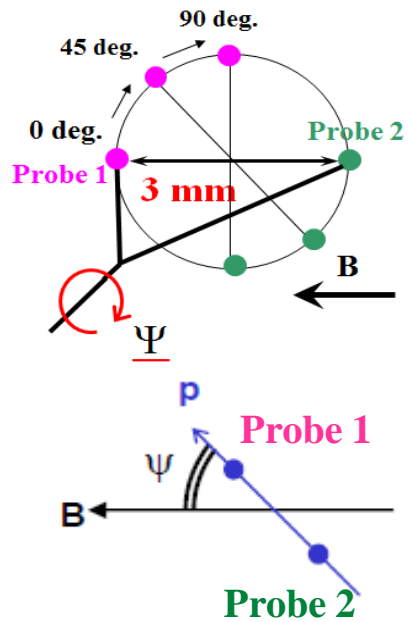


Low-Frequency

It is observed another low-frequency (~ 3.6 kHz) mode when the large ETG is formed.

Identification of a low-frequency fluctuation

$$P_{\mu} = 20 \text{ W}, V_{g1} = -10 \text{ V}, V_{g2} = -30 \text{ V}, V_{ee1} = -4.0 \text{ V}, V_{ee2} = -1.5 \text{ V}, r = -1.5 \text{ cm}, \underline{\Psi} \sim 0^{\circ}$$



Phase shift between \tilde{n} and \tilde{n}

Phase shift between \tilde{n} and $\tilde{\phi}$

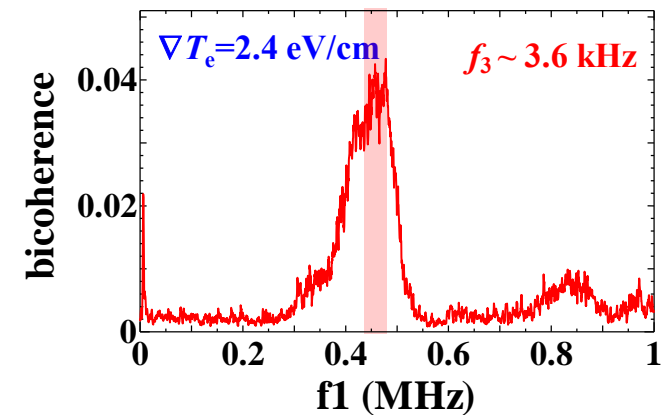
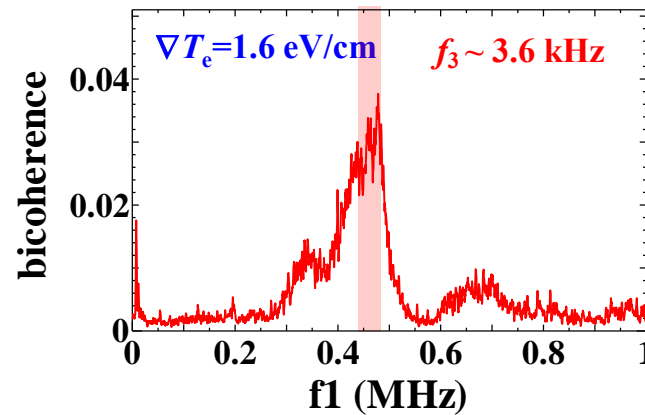
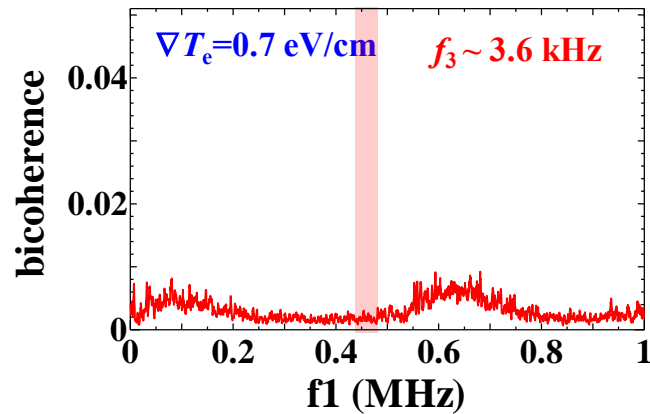
※ Flute mode

① $k_{\parallel} \sim 0$

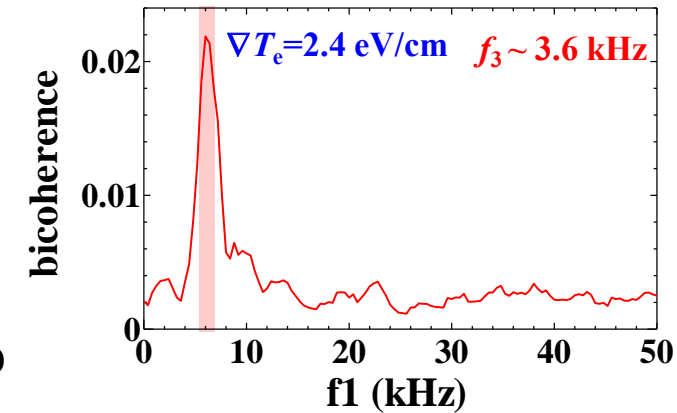
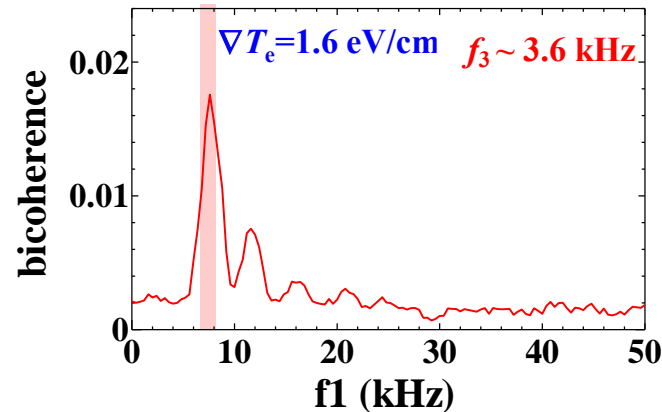
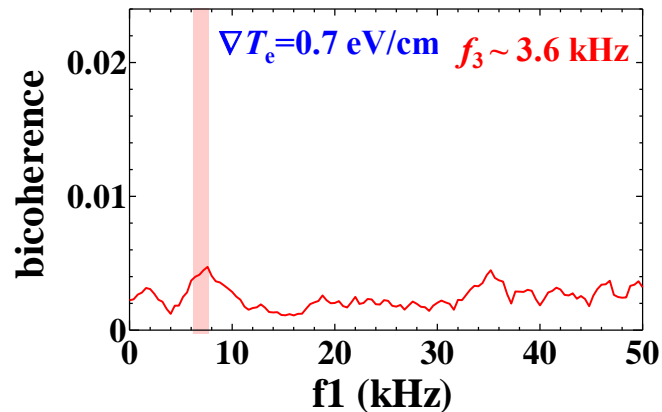
② phase shift between \tilde{n} and $\tilde{\phi}$ is 180 deg.

ETG mode ($f_2 = \sim 0.4$ MHz)

$P_\mu = 20$ W, $V_{g1} = -10$ V, $V_{ee1} = -4.0$ V,
 $V_{ee2} = -1.5$ V, $r = -0.9$ cm



DW mode ($f_2 = \sim 7$ kHz)

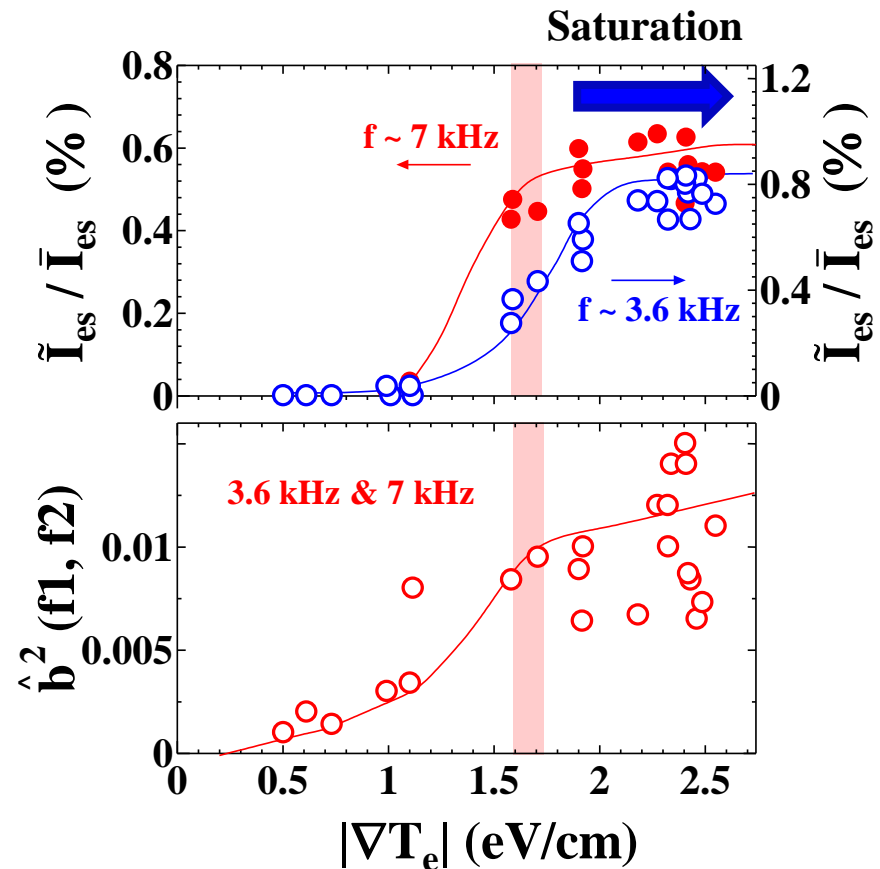
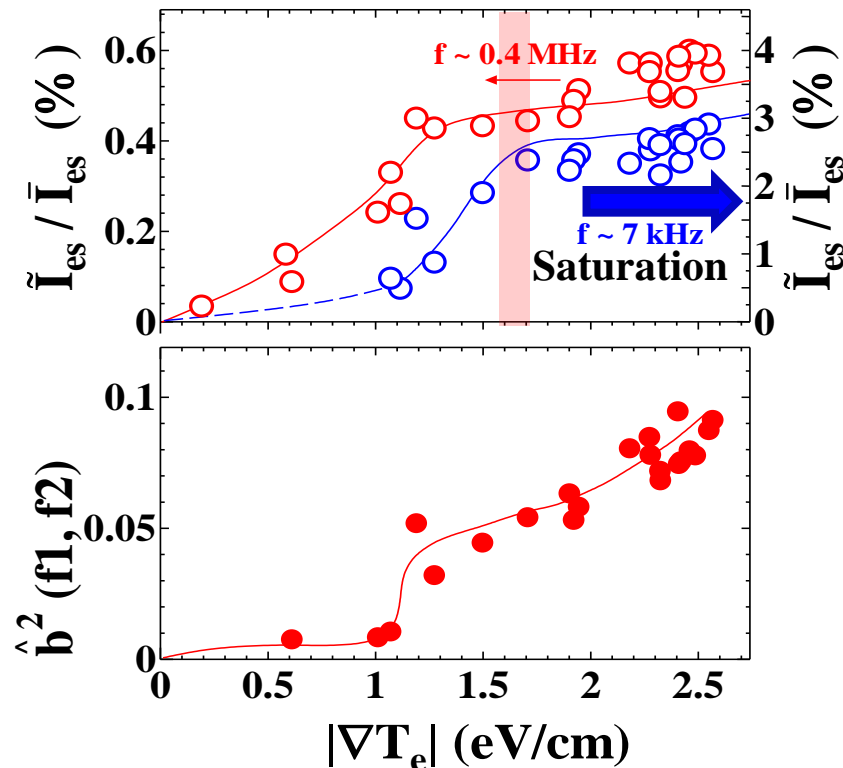


The slice of bicoherence between the DW mode and the flute mode has a noticeable peak when the magnitude of ETG is increased.

Nonlinear Energy Transfer (flute mode)

$$P_{\mu} = 20 \text{ W}, V_{g1} = -10 \text{ V}, V_{ee1} = -4 \text{ V}, V_{ee2} = -1.5 \text{ V}, r = -0.9 \text{ cm}$$

Nonlinear interaction between ETG mode and DW mode



C. Moon, et al., Phys. Plasmas **22**, 052301 (2013).

It is considered that the energy of the DW mode is transferred to the flute mode through the nonlinear interaction.

Free Energy Source (∇T)
ETG

Electron-scale fluctuation

$\sim \rho_e$

Ion-scale fluctuation

$\sim \rho_i$

Device-scale fluctuation

~ 1 kHz

Sat. ($\nabla T_e > \sim 1.2$ eV/cm)
 Inc. ($\nabla T_e > \sim 0.1$ eV/cm)

ETG mode
 (~0.4 MHz)

Anomalous electron heat transport¹⁾

Inc. ($\nabla T_e > \sim 1.2$ eV/cm)
 Sat. ($\nabla T_e > \sim 1.7$ eV/cm)

Drift wave mode²⁾
 (~7 kHz)

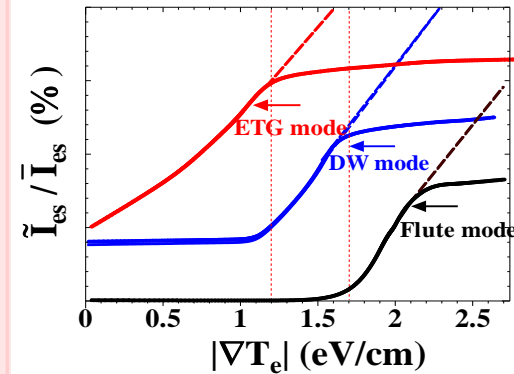
Energy Transfer

Flute mode³⁾
 (~3.6 kHz)

Inc. ($\nabla T_e > \sim 1.7$ eV/cm)
 Sat. ($\nabla T_e > \sim 2.2$ eV/cm)

? ~1 kHz

• Streamers⁴⁾
 • Zonal flow⁵⁾



Fluctuations Level as a Function of the ETG

Anomalous heat transport⁶⁾

References

- 1) F. Ryter, et al., Phys. Rev. Lett. **86**, 5498 (2001).
- 2) C. Moon, et al., Phys. Rev. Lett. **111**, 115001 (2013).
- 3) C. Moon, et al., Phys. Plasmas **22**, 115001 (2015).
- 4) T. Yamada, et al., Phys. Rev. Lett. **105**, 225002 (2010).
- 5) Y. Nagashima, et al., Phys. Plasmas **16**, 020706 (2009).
- 6) S.-I. Itoh and K. Itoh, Plasma Phys. Control. Fusion **43**, 1055 (2001).

In order to understand the electron temperature gradient (ETG) mode driven anomalous heat transport, we investigate a multi-scale nonlinear coupling between the electron-scale ETG mode and the ion-scale fluctuations in linear magnetized plasmas.

- The formed ETG is found to excite a high-frequency fluctuation (~ 0.4 MHz), i.e., ETG mode, furthermore, the drift wave (DW) mode (~ 7 kHz), which is enhanced by the nonlinear coupling with the ETG mode.
- It is observed another low-frequency (~ 3.6 kHz) fluctuation associated with the flute mode is enhanced by the nonlinear coupling with the DW mode.
- The ETG mode energy was transferred to the DW mode, and then the energy was ultimately transferred to the flute mode, which was triggered by the disparate scale nonlinear interactions between the ETG and ion-scale low-frequency modes.



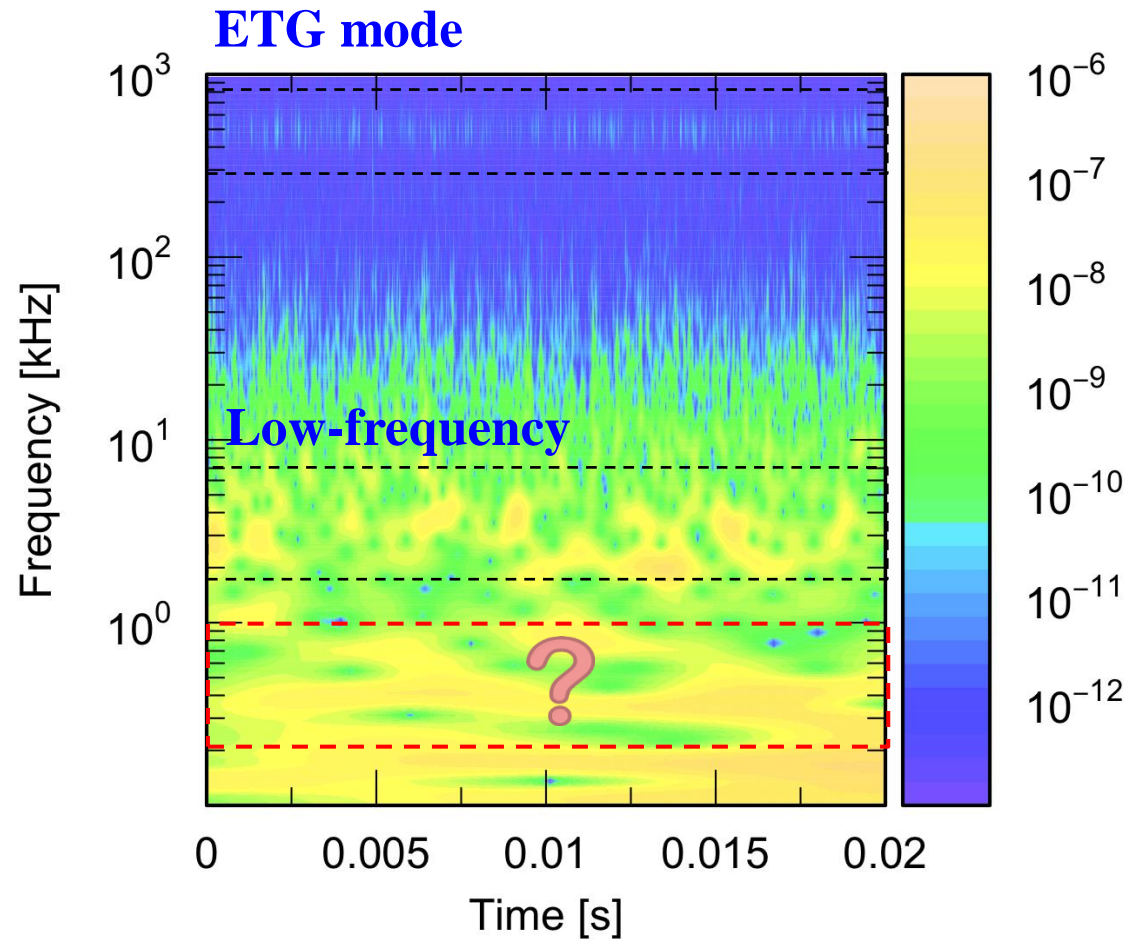
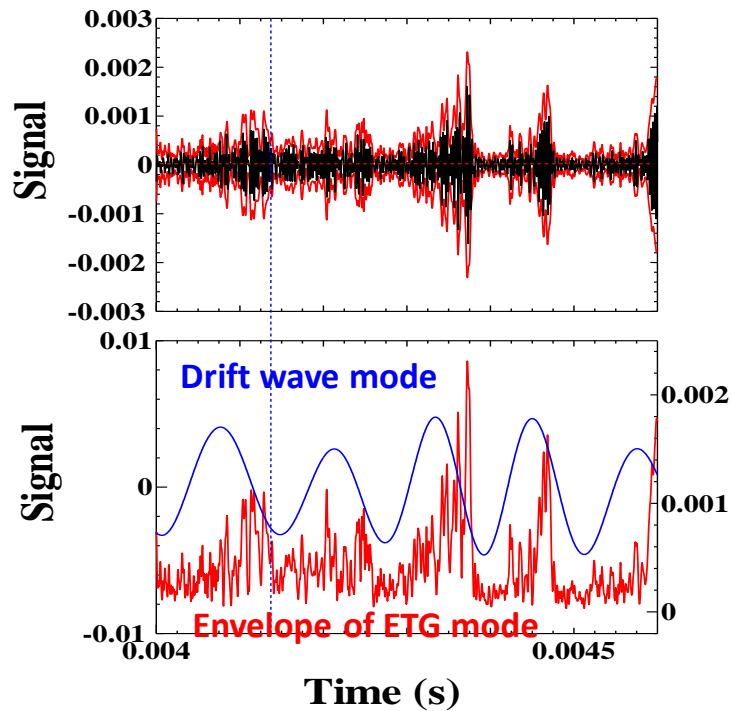
Acknowledgements

The authors acknowledge helpful discussions by Prof. S. Inagaki and Prof. S.-I. Itoh. This work was supported by the Grant-in-Aid for JSPS Fellows (23-1638), and a Grant-in-Aid for Scientific Research from the Ministry of Education, Culture, Sports, Science and Technology, Japan. This work was partly supported by the Grant-in-Aid for Scientific Research of JSPF, Japan (Nos. 15H02155 and 23244113), by the collaboration programs of the RIAM of Kyushu University and of NIFS (NIFS13KOCT001), and by the Asada Science Foundation.

$$P_{\mu} = 20 \text{ W}, V_{ee1} = -4 \text{ V}$$
$$V_{ee2} = -1.5 \text{ V}, V_{g1} = -10 \text{ V}$$
$$r = -1.5 \text{ cm}, \nabla T_e = 2.4 \text{ eV/cm}$$

— DW mode (~ 7 kHz filtering)
— Envelope of ~ 0.4 MHz fluctuations

Envelope & Filter

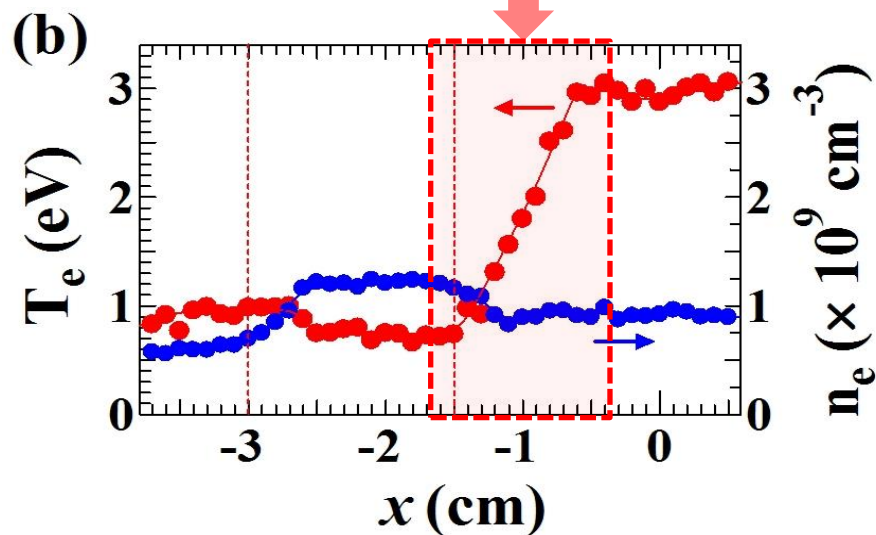


The modulation of ETG mode with low-frequency fluctuations is well observed when sufficient ETG is formed.

プラズマの半径方向分布

$P_{\mu} = 20 \text{ W}$, $V_{g1} = -10 \text{ V}$, $V_{g2} = -30 \text{ V}$,
 $V_{ee1} = -4.0 \text{ V}$, $V_{ee2} = -1.5 \text{ V}$, $r = -1.5 \text{ cm}$

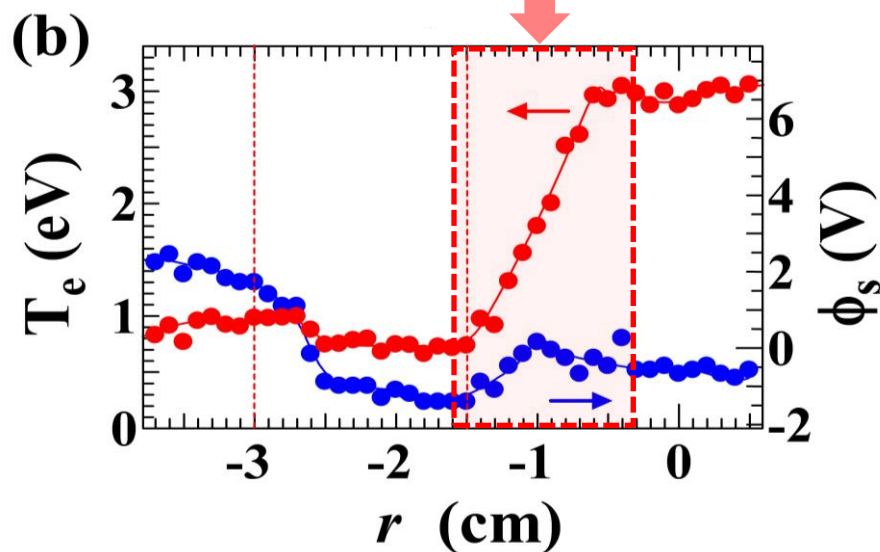
PRL2013の図1



電子密度勾配が谷のように形成

$$\left| \frac{n_e'}{n_e} \right| = 14.5 \text{ m}^{-1}$$

POP2015の図2

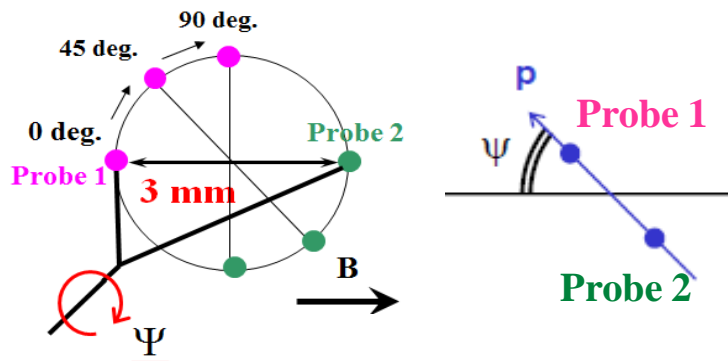


$E_r \approx +0.1 \text{ (V/cm)}$

$E \times B$ 方向はイオン反磁性方向

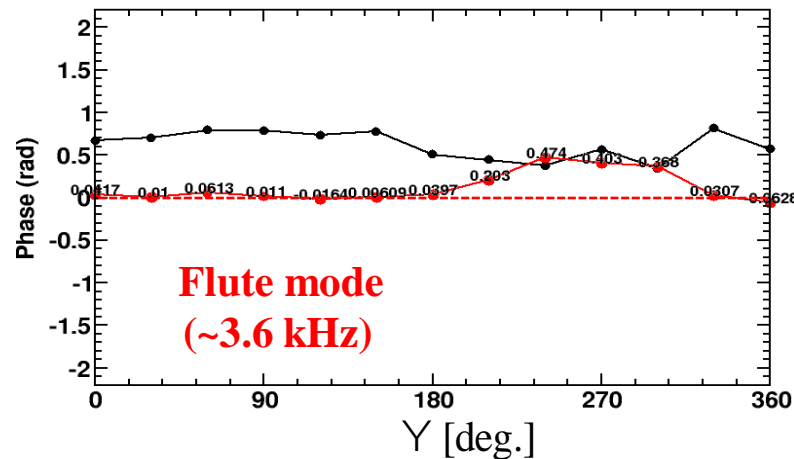
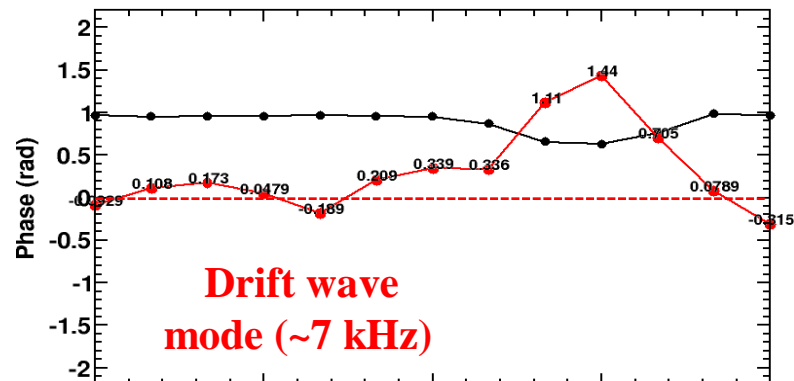
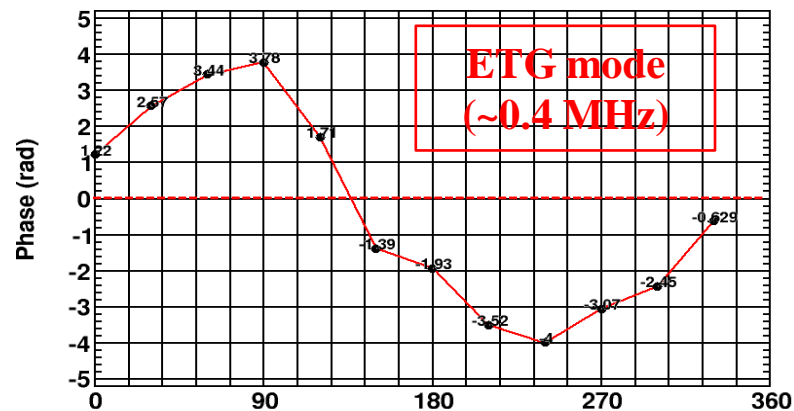
位相差測定によるモード数の同定(密度揺動のみ)

$P_{\mu} = 20 \text{ W}$,
 $V_{g1} = -10 \text{ V}$,
 $V_{g2} = -30 \text{ V}$,
 $V_{ee1} = -4.0 \text{ V}$,
 $V_{ee2} = -1.5 \text{ V}$,
 $r = -1.5 \text{ cm}$

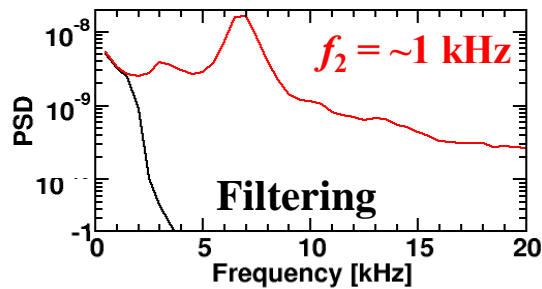
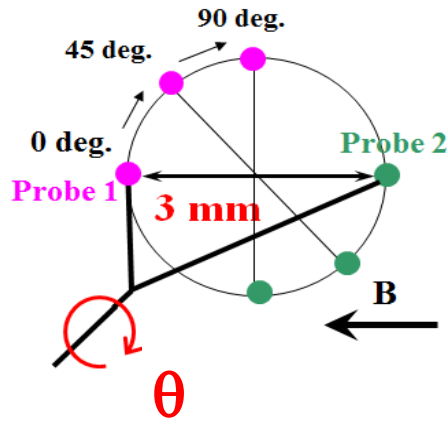
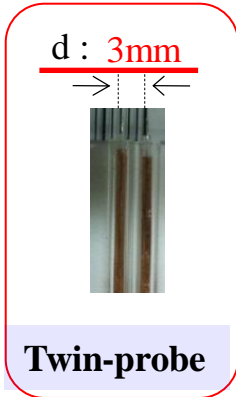


磁場に垂直(θ)方向への伝搬方向とそのモード数

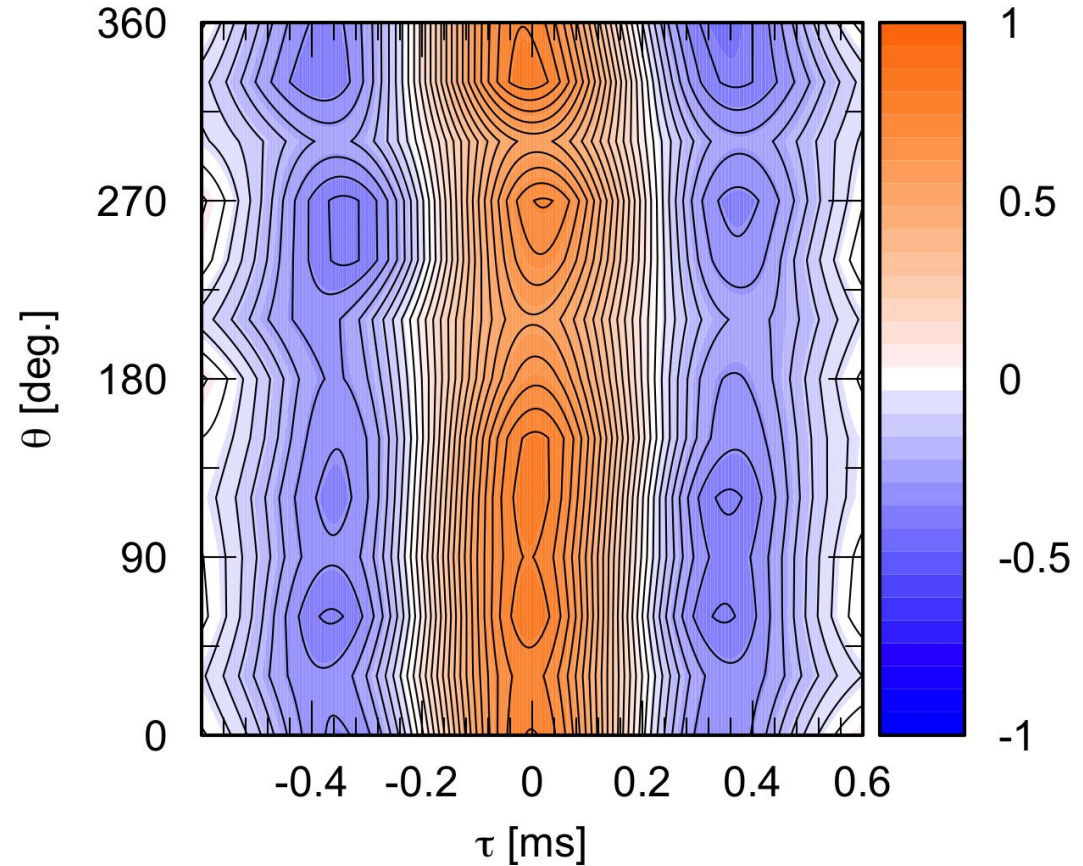
	ETG	DW	flute
mode number	~40	~8	~2
波長 λ (mm)	~2.4	~11.5	~44.9
周波数 f (kHz)	460	7	3.6
伝搬方向	電子反磁性	イオン反磁性(?)	イオン反磁性(?)



$$P_{\mu} = 20 \text{ W}, V_{g1} = -10 \text{ V}, V_{ee1} = -4.0 \text{ V}, V_{ee2} = -1.5 \text{ V}, \\ V_{g2} = -30 \text{ V} (\nabla T_e = 2.4 \text{ eV/cm}).$$

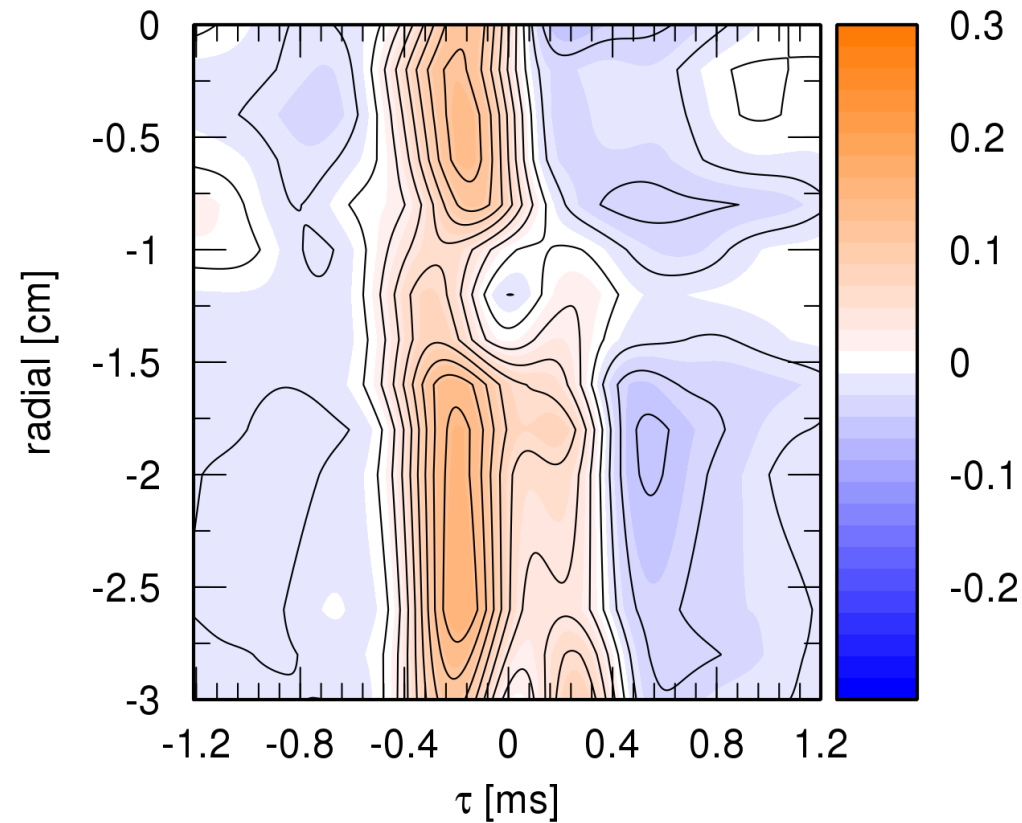
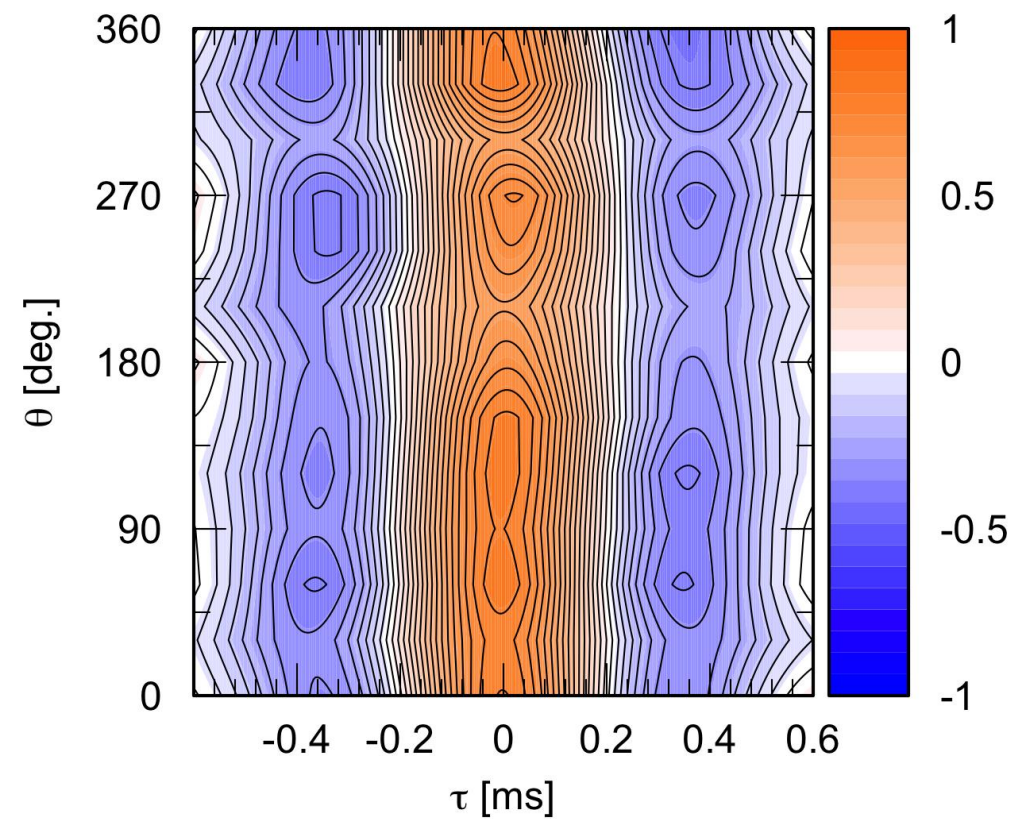


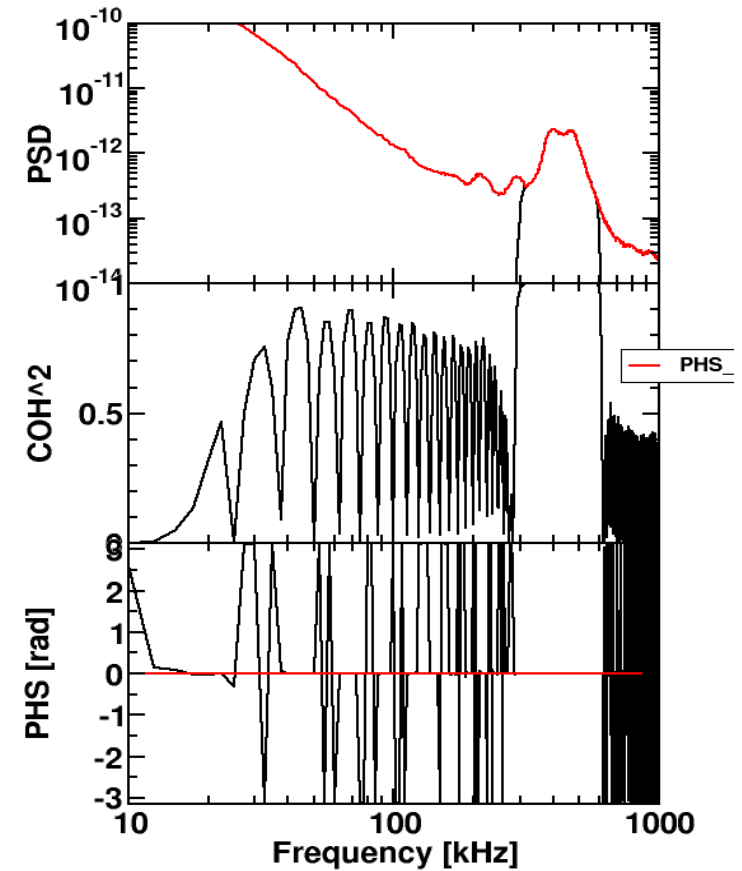
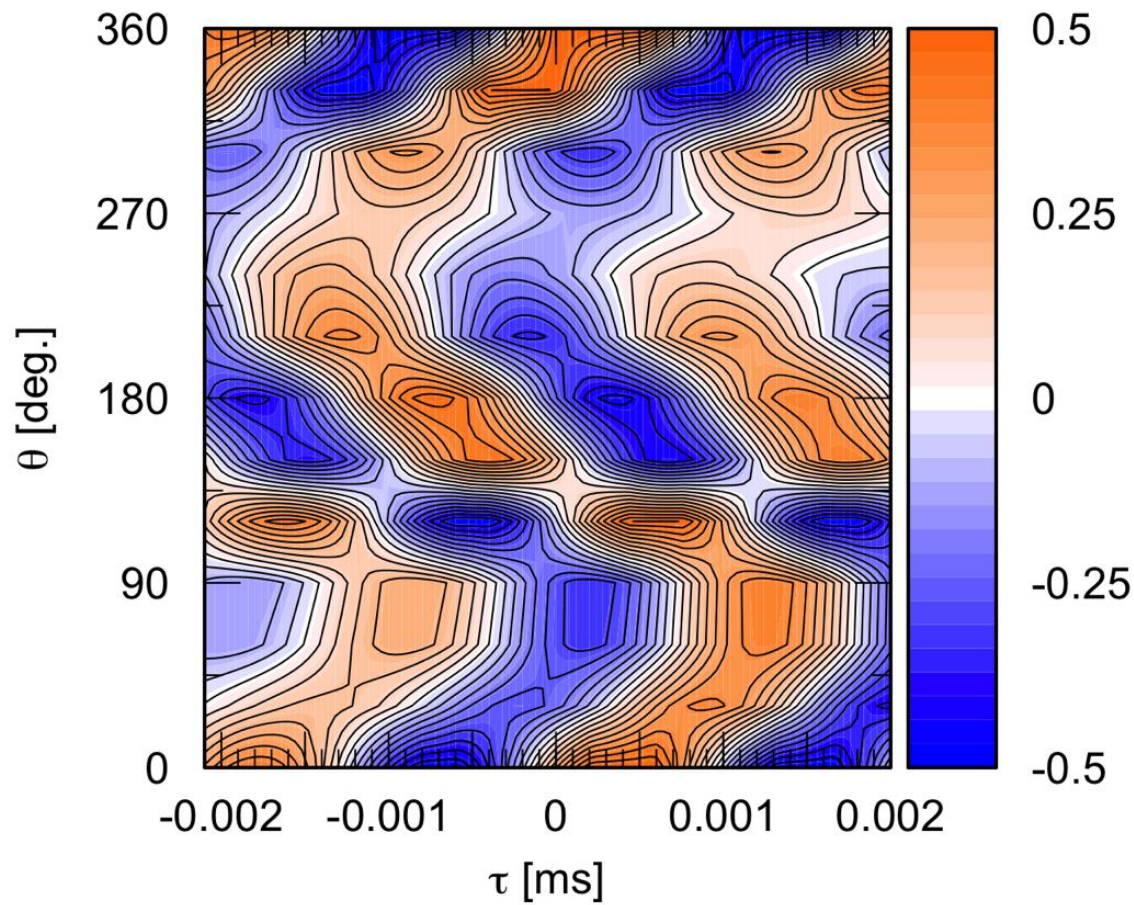
Cross-Correction with \tilde{n} and \tilde{n}



It is found that the fluctuations with $f \approx 1 \text{ kHz}$ is the poloidal wave number $k_{\theta} = 0$ ($m \sim 0$).

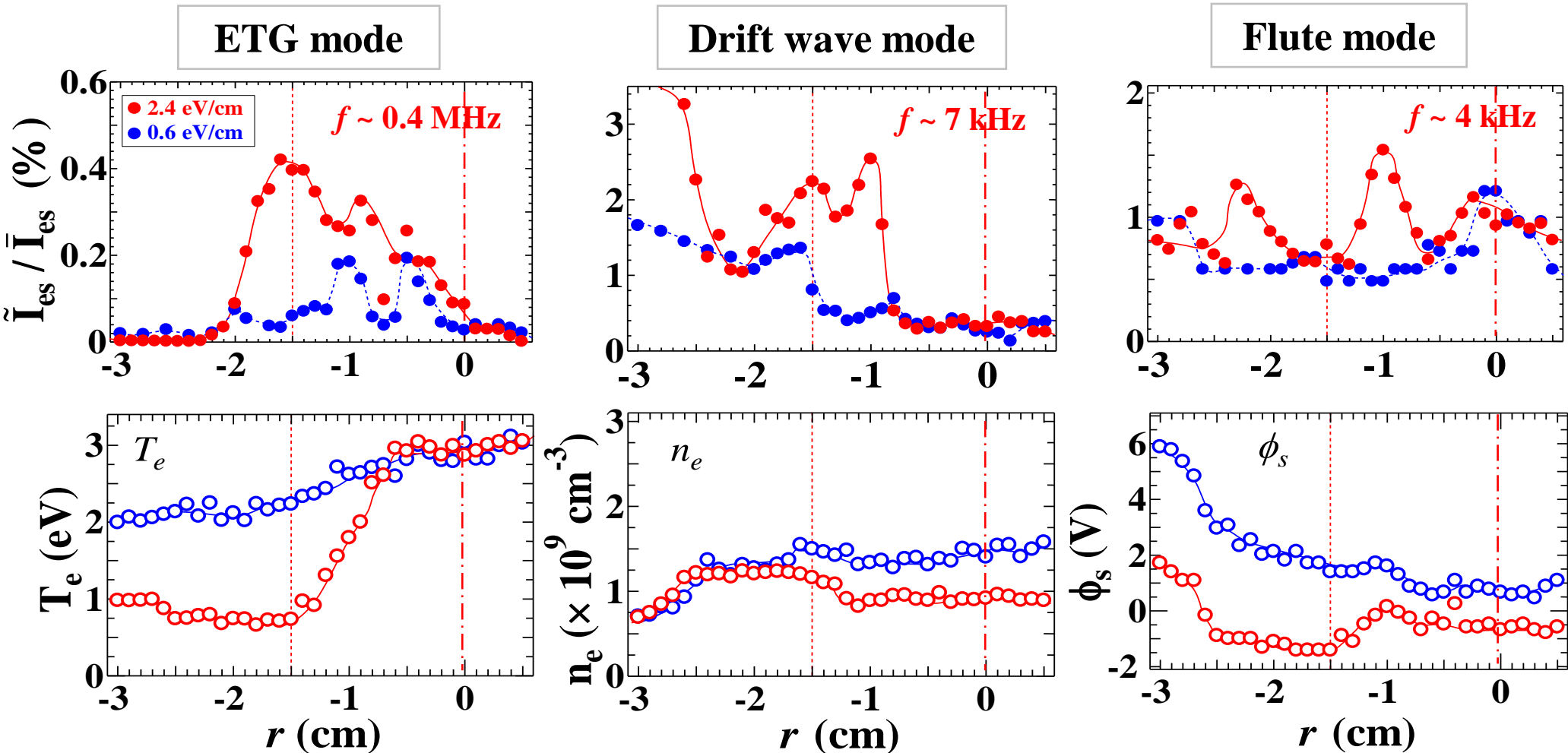
Cross-Correlation with \tilde{n} and \tilde{n}





Radial Profiles of ETG driven Fluctuations

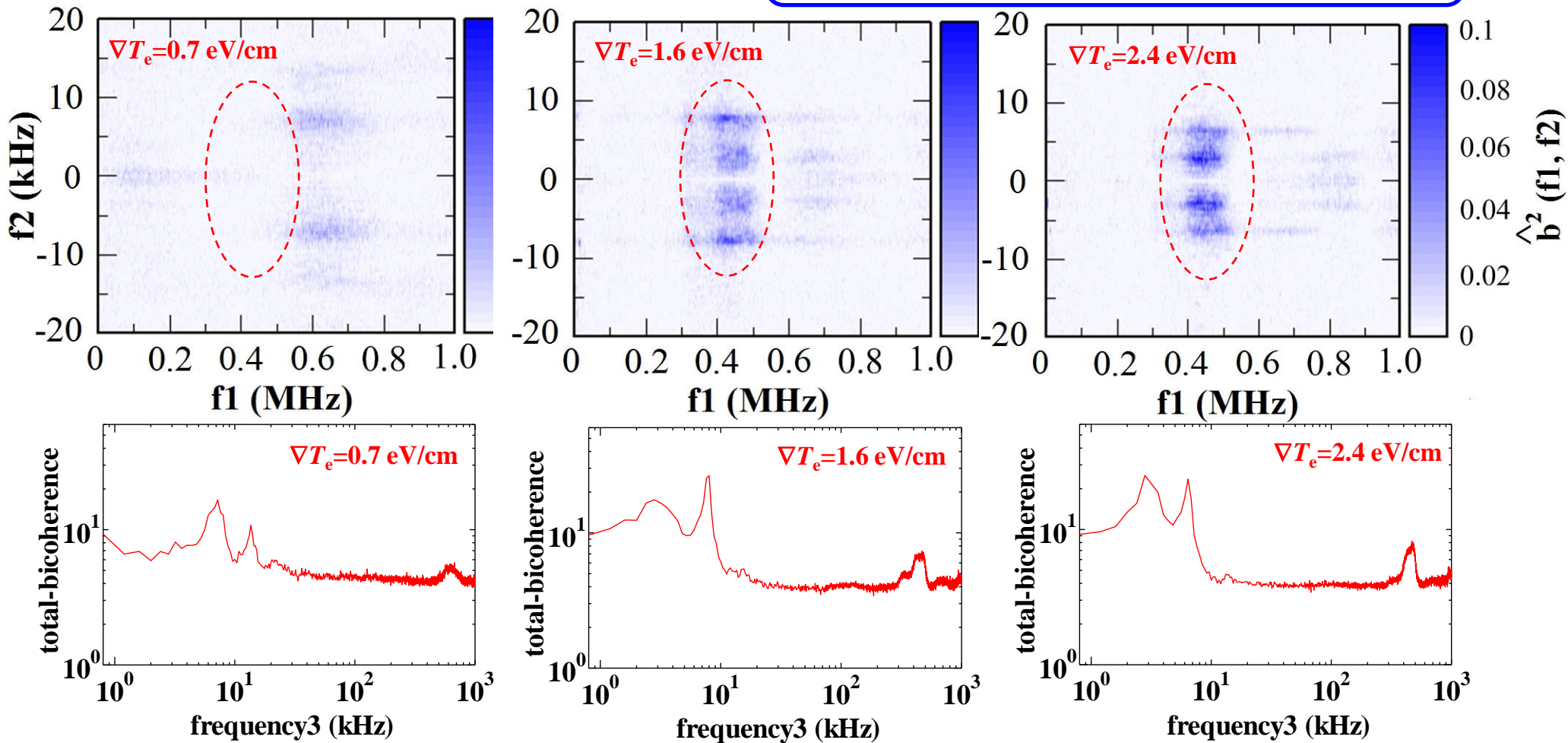
$$P_{\mu} = 20 \text{ W}, V_{g1} = -10 \text{ V}, V_{g2} = -30 \text{ or } 3 \text{ V}, V_{ee1} = -4 \text{ V}, V_{ee2} = -1.5 \text{ V}$$



It is observed another low-frequency (~ 4 kHz) mode when the electron temperature gradient ∇T_e exceeds a certain threshold.

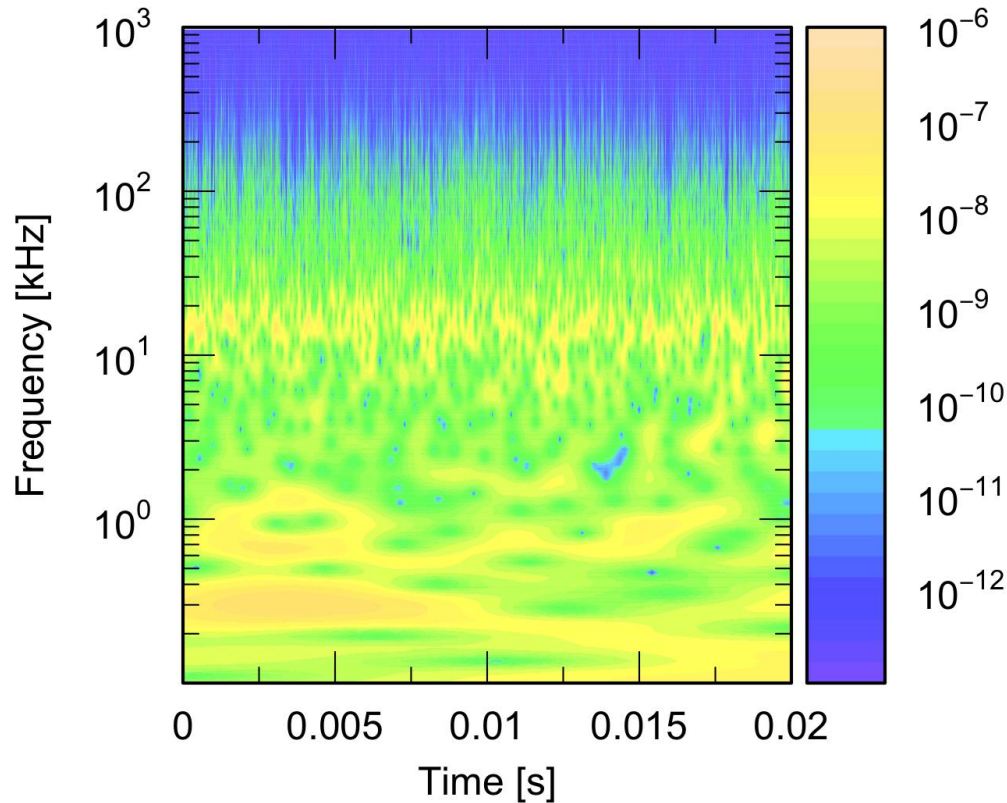
Squared Bicoherence

$$P_{\mu} = 20 \text{ W}, V_{g1} = -10 \text{ V}, V_{ee1} = -4.0 \text{ V}, \\ V_{ee2} = -1.5 \text{ V}, r = -0.9 \text{ cm}$$

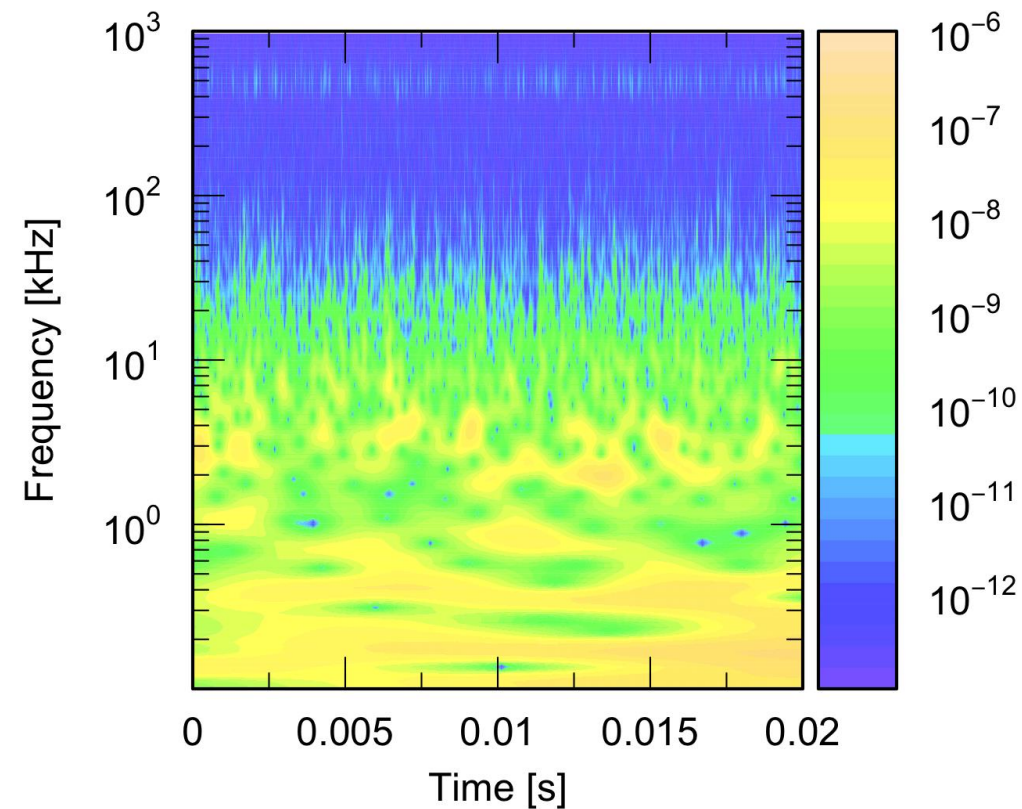


The nonlinear couplings between the ETG mode and the ion-scale Fluctuations become stronger as the magnitude of ETG is increased.

$$P_{\mu} = 20 \text{ W}, V_{ee1} = -4 \text{ V}, V_{ee2} = -1.5 \text{ V}, V_{g1} = -10 \text{ V}, r = -1.5 \text{ cm}$$



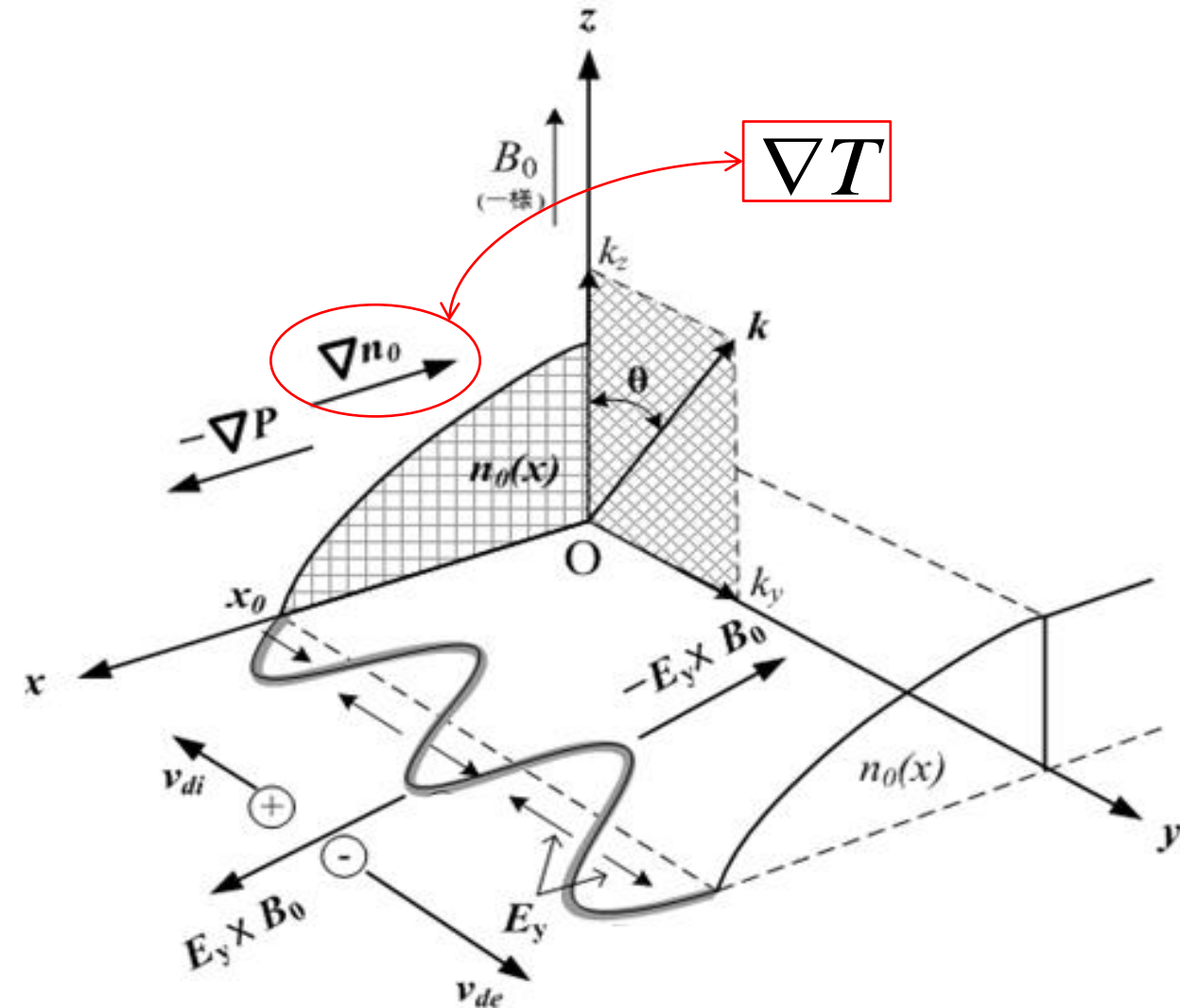
$$\nabla T_e = 0.7 \text{ eV/cm}$$



$$\nabla T_e = 2.4 \text{ eV/cm}$$

The modulation of ETG mode with low-frequency fluctuations is well observed when sufficient ETG is formed.

付録 1: ETGモードの機構



- 圧力勾配による力 F

$$F = -\nabla p_{e,i} / n_0 = -kT_{e,i} \nabla n_0 / n_0$$

$$p = nkT$$

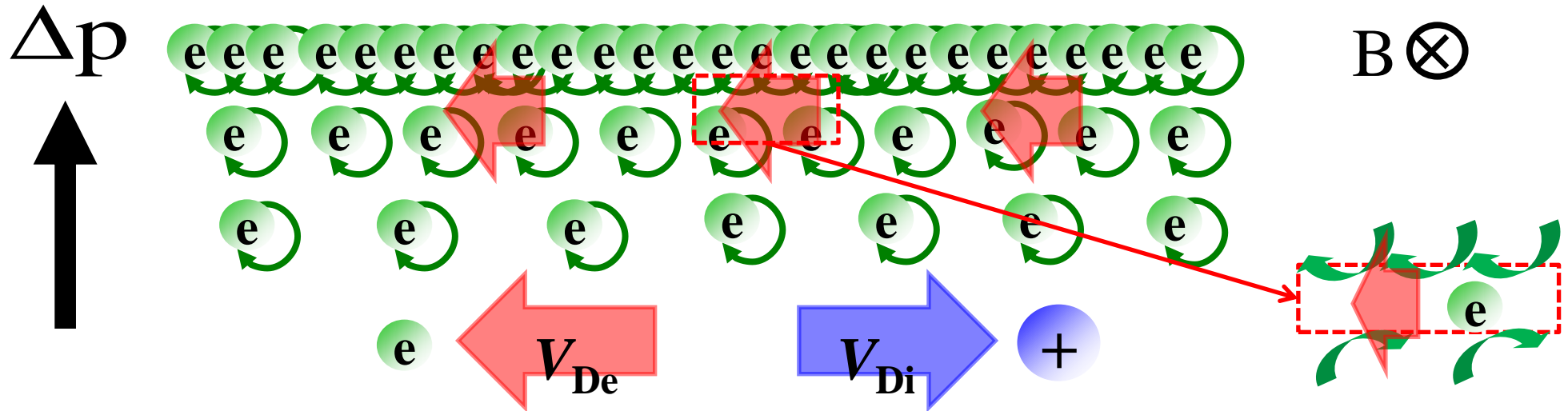
ドリフト不安定性場合

$$\nabla p = Tk \nabla n$$

- ① わずがの波状の外乱.
- ② 正負電荷のドリフト運動が発生.
- ③ 荷電分離が生じて電界Eが誘起.
- ④ $E \times B$ ドリフトによってxの正負両方向に波状の変位が助長される.

ETG 不安定性場合

$$\nabla p = nk \nabla T$$



プラズマの圧力によって各粒子が受ける力は

$$F = -\frac{1}{n} \nabla p$$

これは(仮想的な)反磁性ドリフトである。
これはイオンと電子に対してドリフトの
方向が異なるため電流を生ずる。

$$V_{de} = -\frac{B \times \nabla p}{enB^2} = \frac{k_b T_e}{eB} \frac{n'}{n} = \frac{k_b T_e}{eB} \frac{T_e'}{T_e}$$

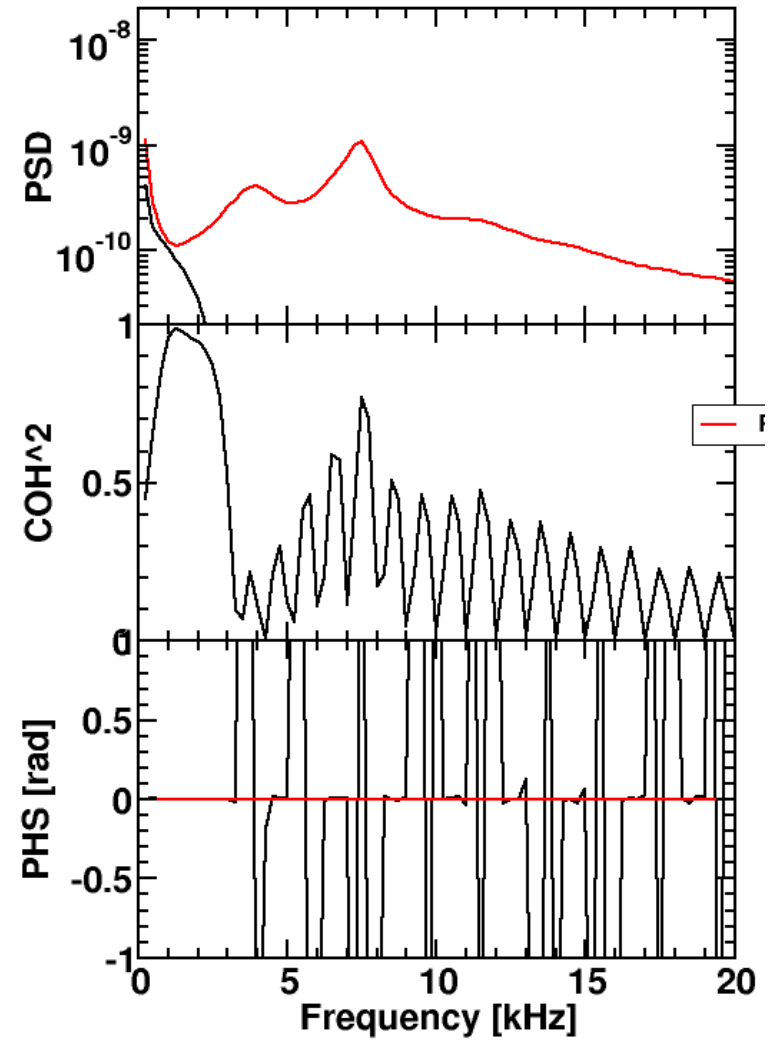
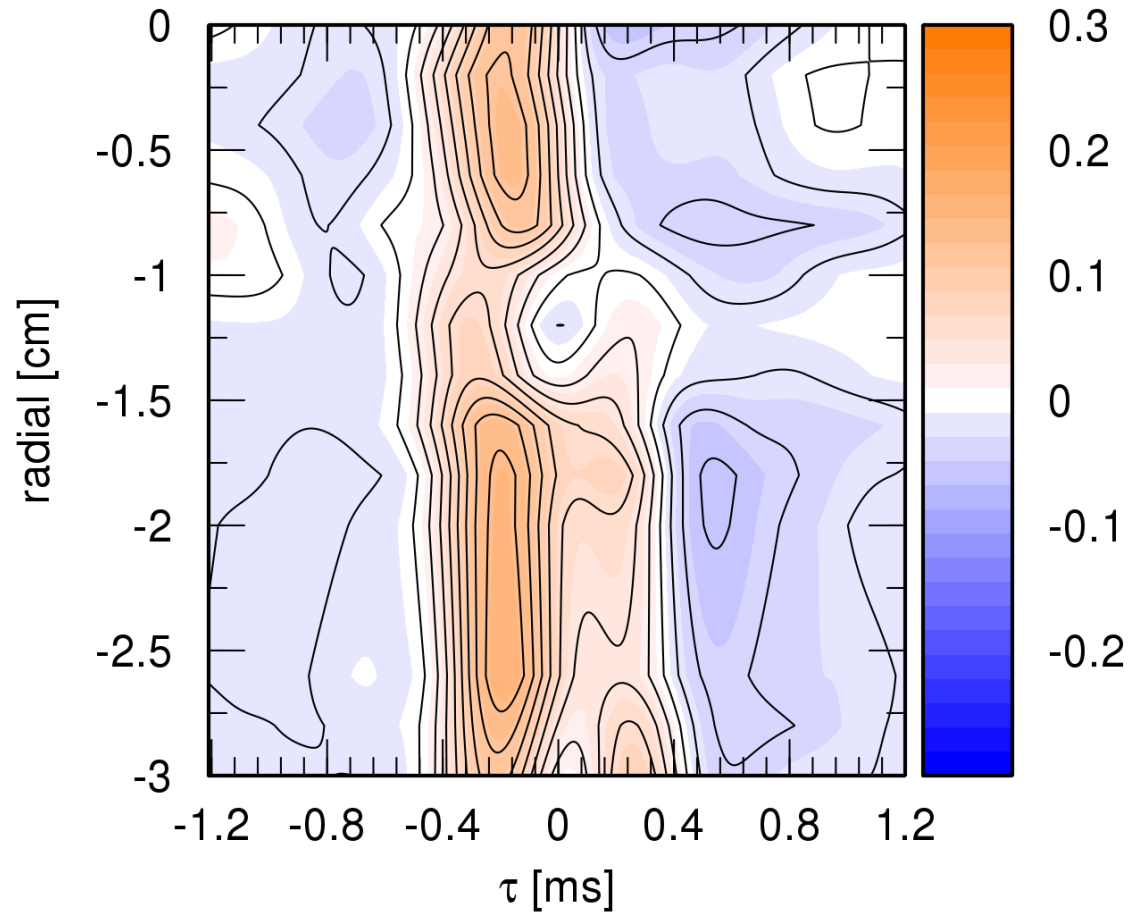
$$V_{di} = -\frac{B \times \nabla p}{enB^2} = \frac{k_b T_e}{eB} \frac{n'}{n} = \frac{k_b T_e}{eB} \frac{T_e'}{T_e}$$

これから反磁性電流は

$$j_D = ne(v_{Di} - v_{De}) = k_B(T_i + T_e) \frac{B \times \nabla n}{B^2}$$

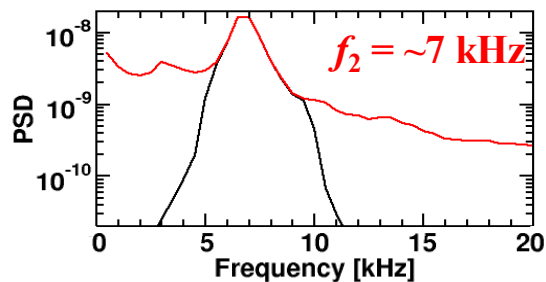
We investigate the effects of the radial electric field (E_r) on suppression of ETG mode through multiscale nonlinear interactions in linear magnetized plasmas.

- The formed ETG is found to excite a high-frequency fluctuation (~ 0.4 MHz), i.e., ETG mode, furthermore, the drift wave (DW) mode (~ 7 kHz), which is enhanced by the nonlinear coupling with the ETG mode.
- It is found that a sufficiently large E_r ($E \times B$ velocity shear) can suppress the ETG mode regardless of its signs.
- The ETG mode amplitude is decreased by the energy transfer of ETG mode to DW mode through the multi-scale non-linear coupling in the slightly negative E_r .

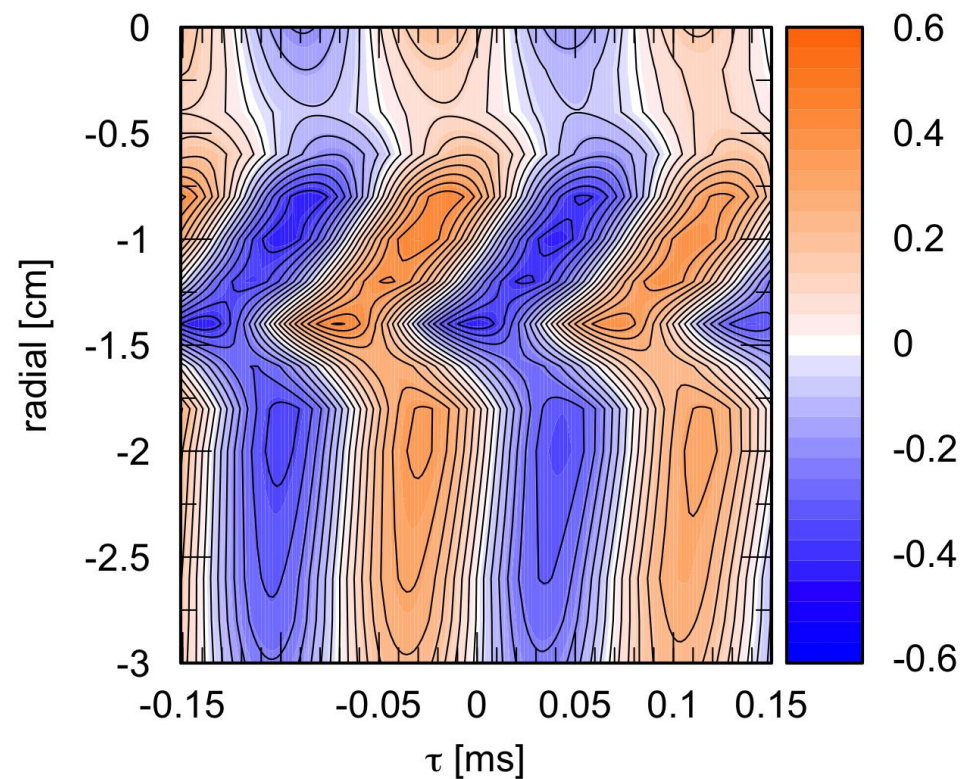
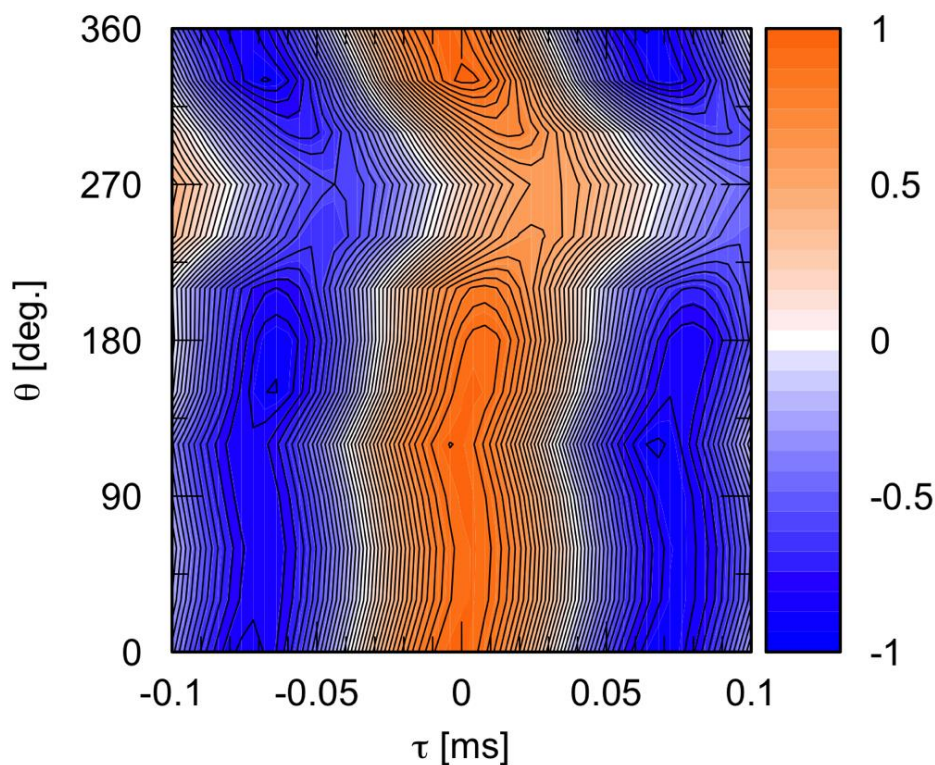


We investigate the effects of the radial electric field (E_r) on suppression of ETG mode through multiscale nonlinear interactions in linear magnetized plasmas.

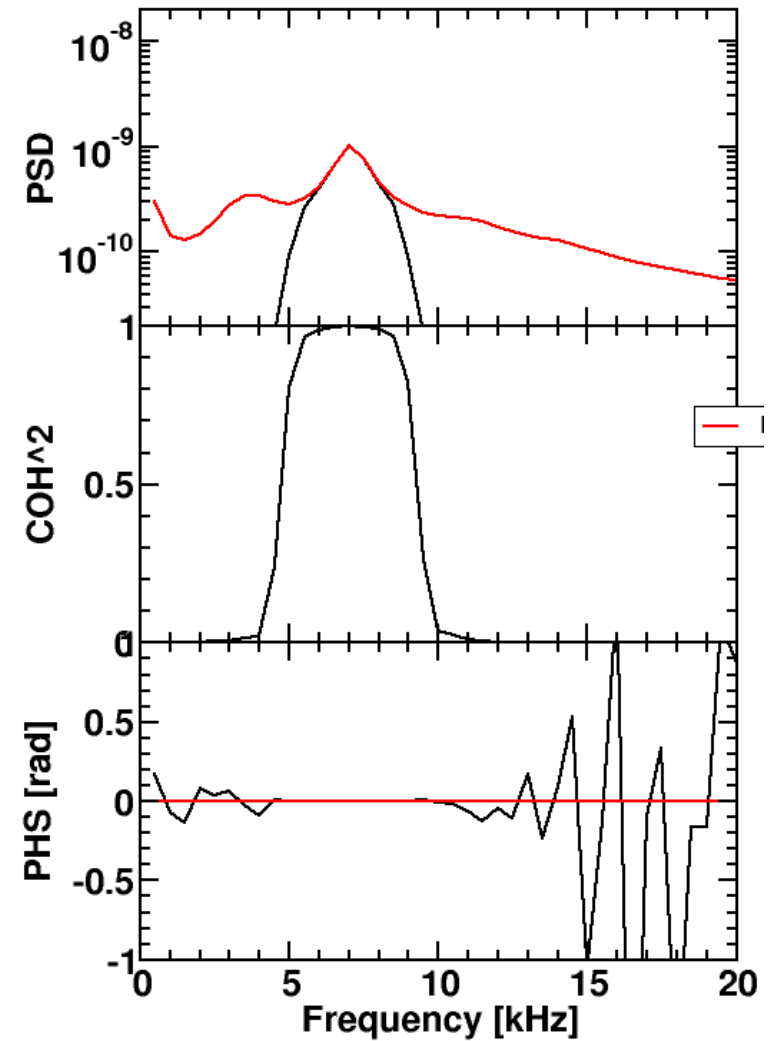
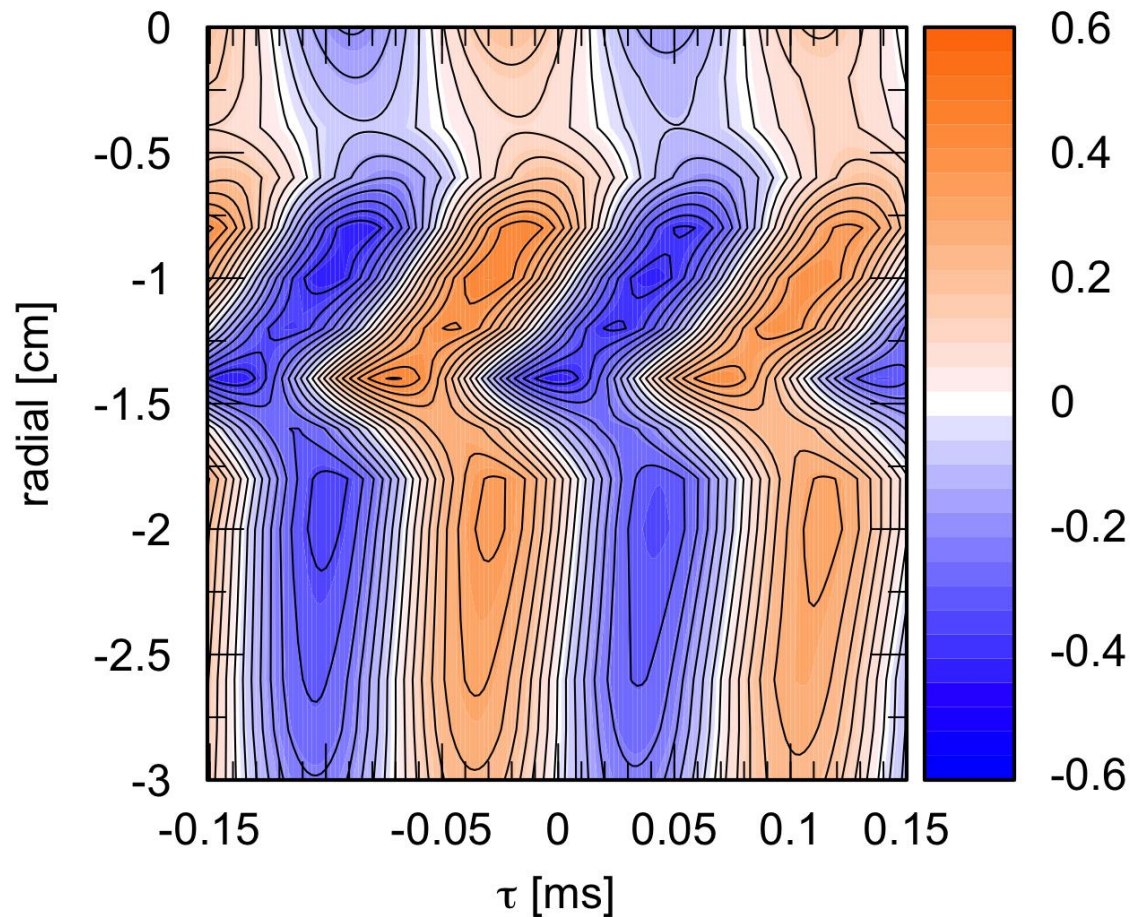
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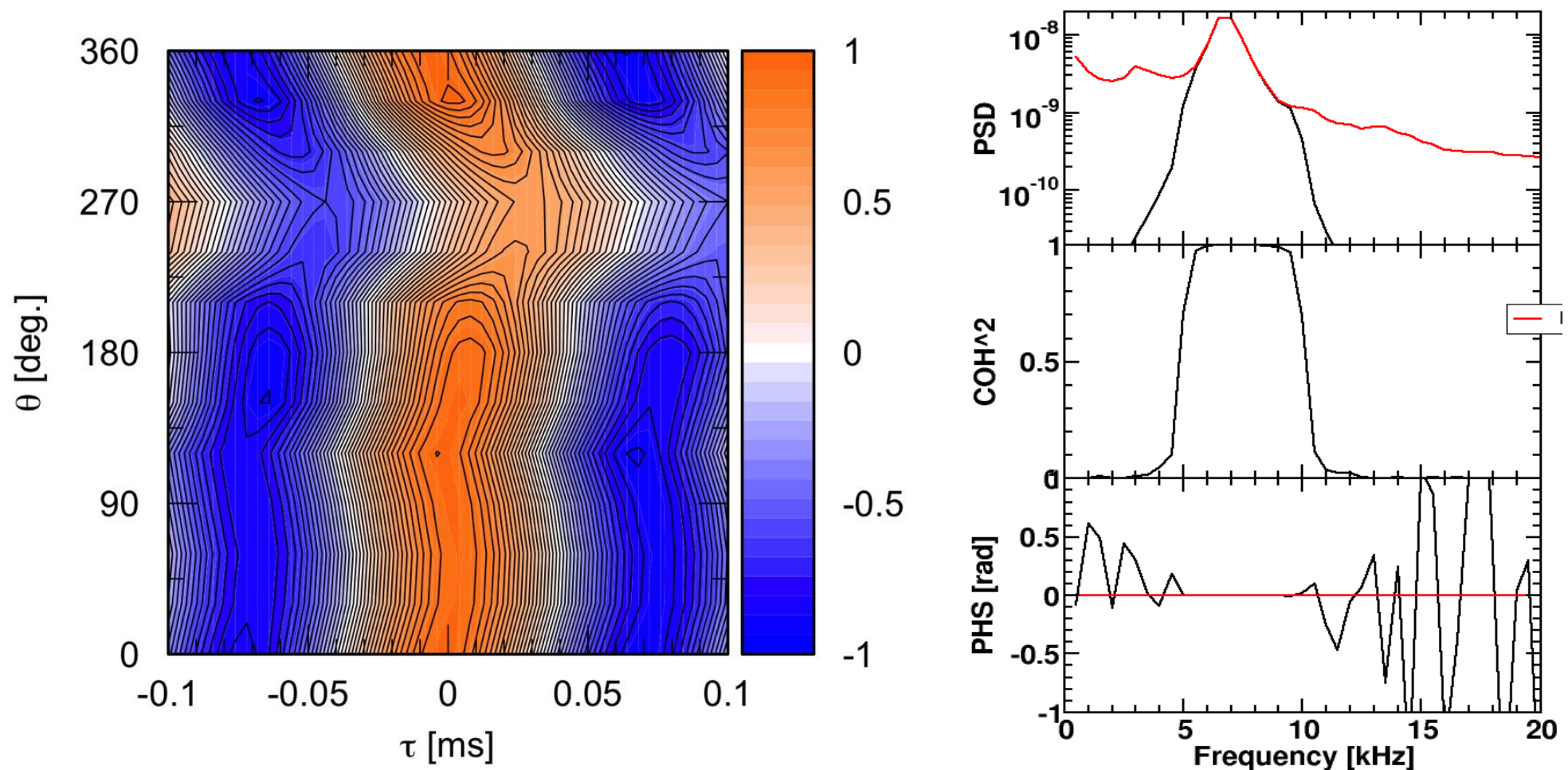
$$P_{\mu} = 20 \text{ W}, V_{g1} = -10 \text{ V}, V_{ee1} = -4.0 \text{ V}, V_{ee2} = -1.5 \text{ V}, \\ V_{g2} = -30 \text{ V} (\nabla T_e = 2.4 \text{ eV/cm}).$$



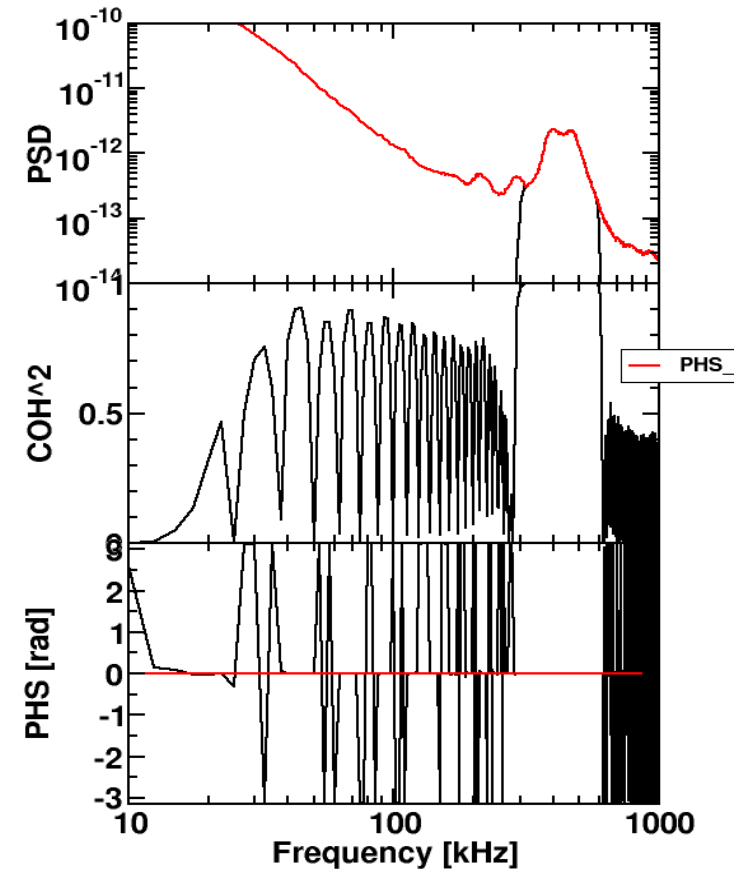
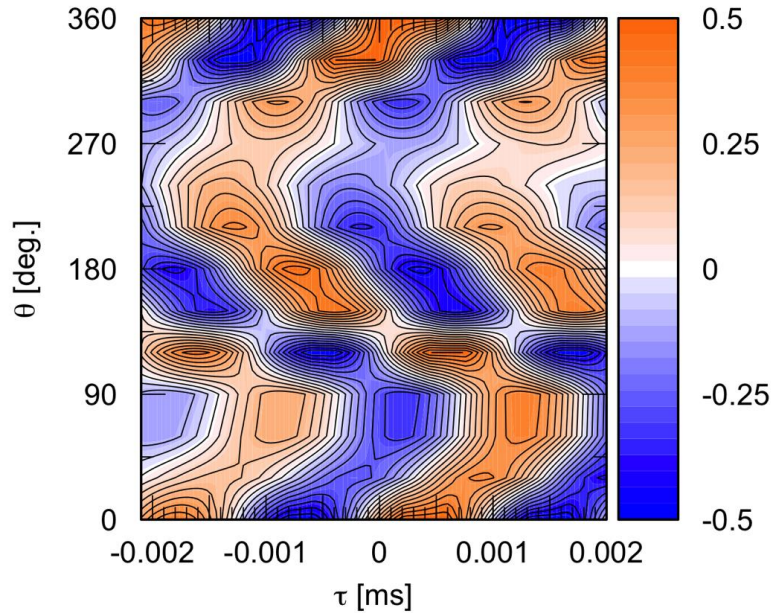
It is found that the fluctuations with $f \simeq 7$ kHz is parallel wave number $k_{\parallel} = 0$ that the energy of the DW mode is transferred to the flute mode through the nonlinear interaction.



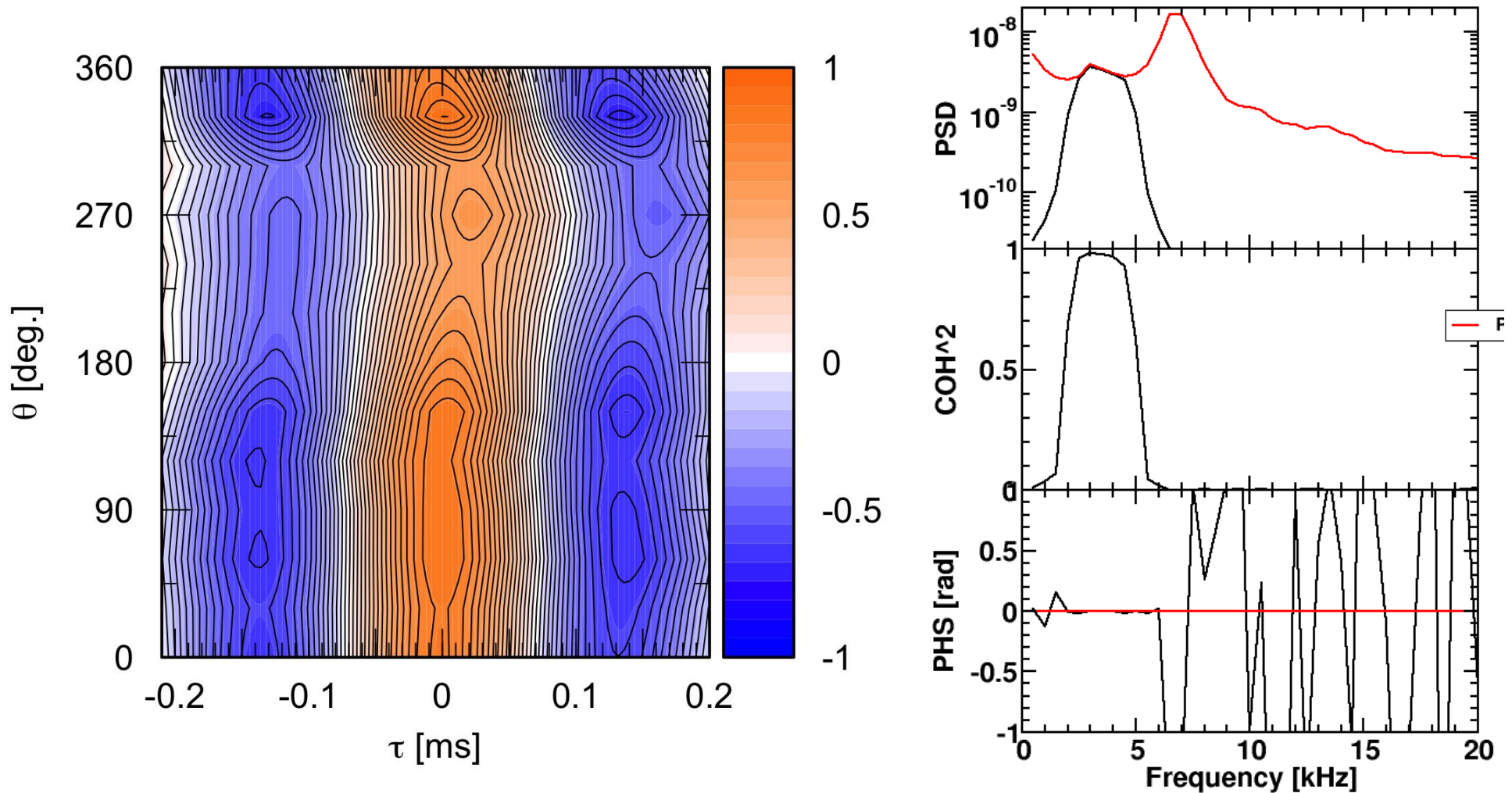
It is considered that the energy of the DW mode is transferred to the flute mode through the nonlinear interaction.



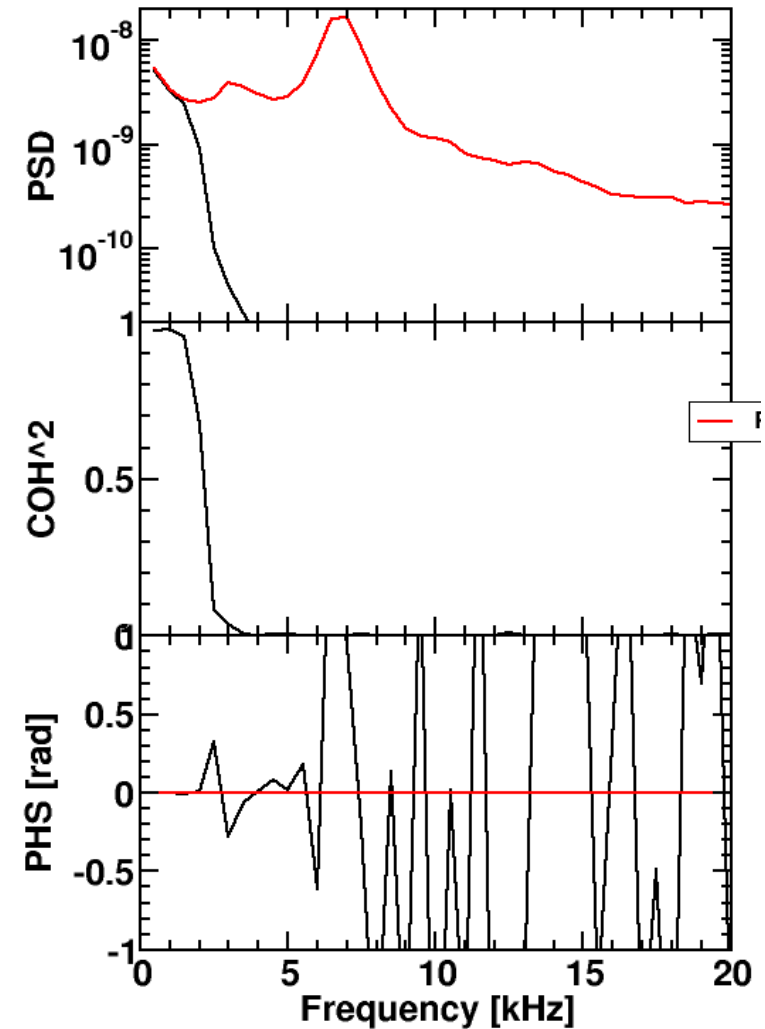
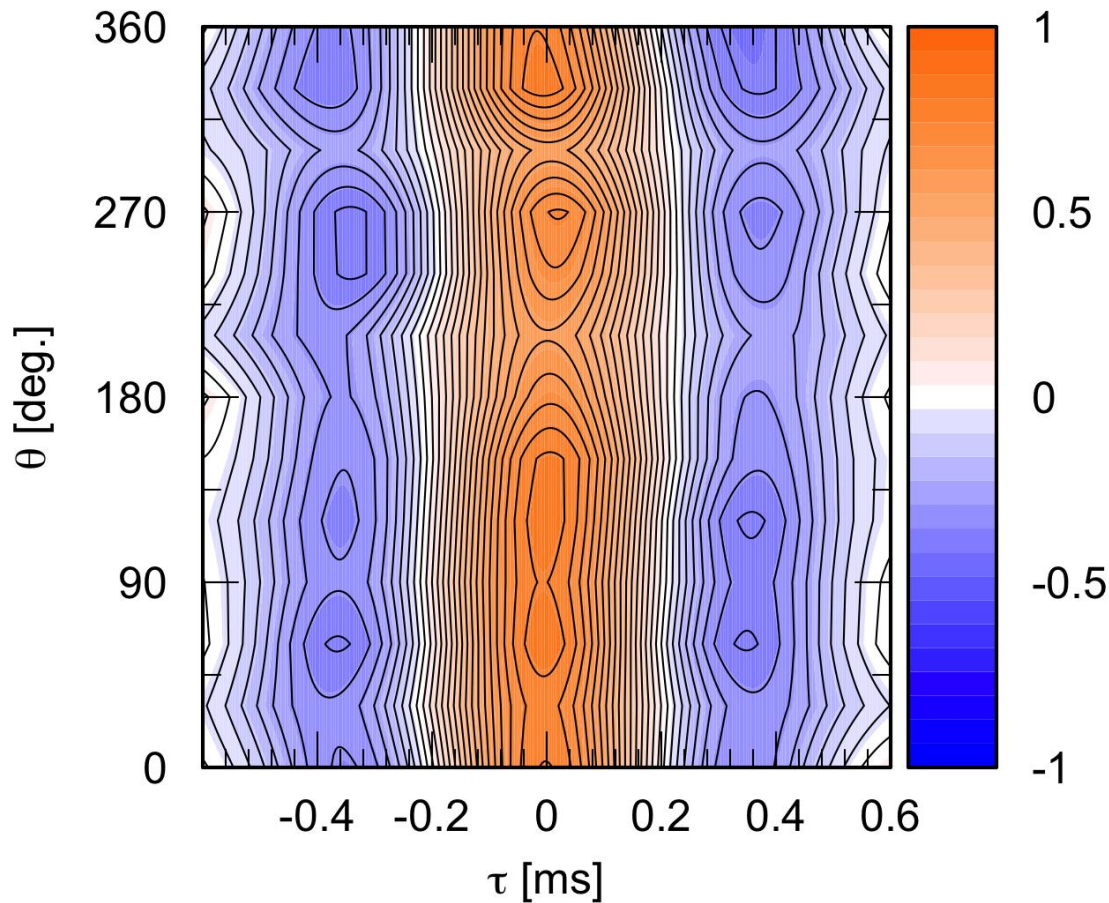
It is considered that the energy of the DW mode is transferred to the flute mode through the nonlinear interaction.



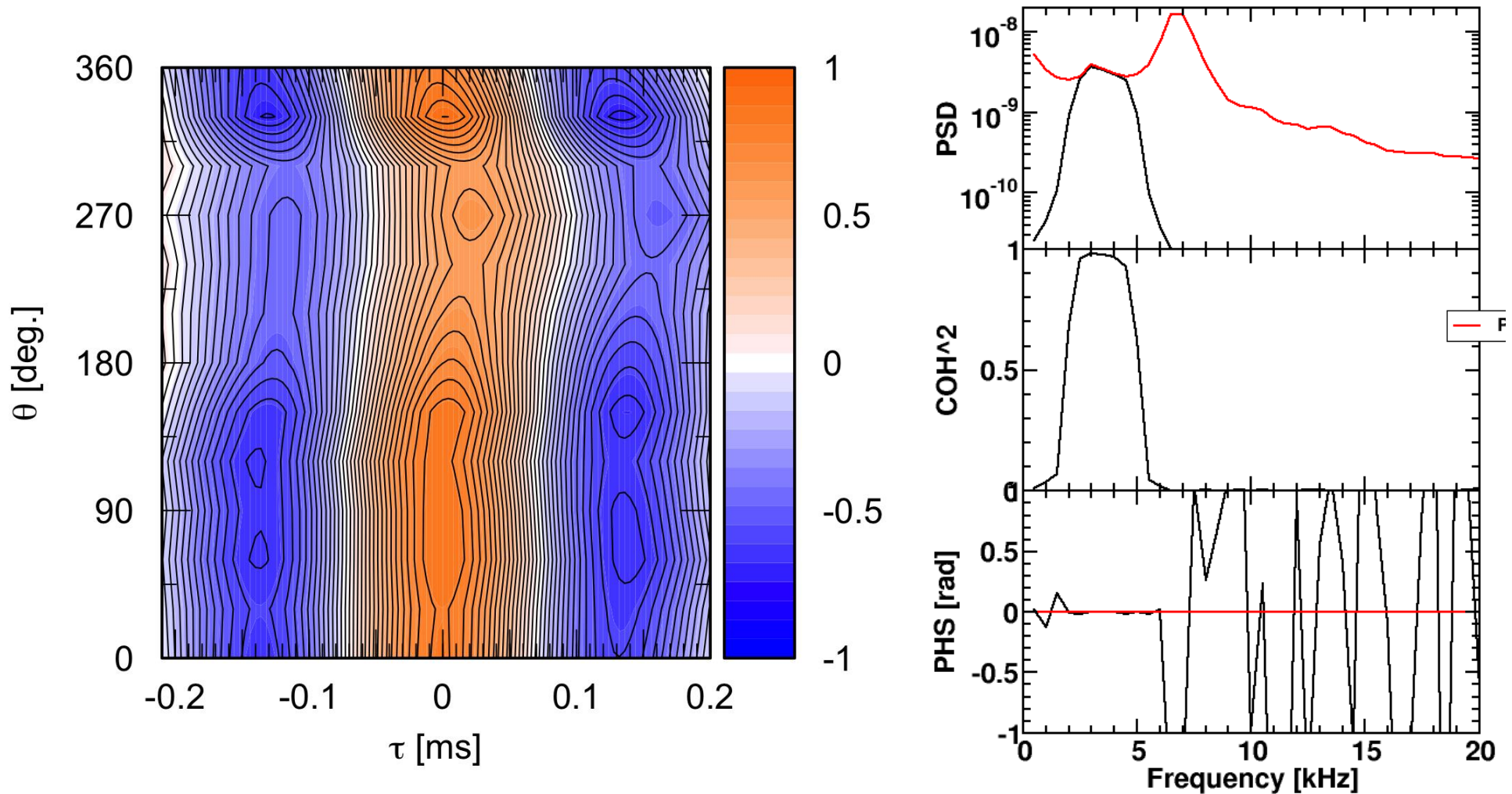
It is considered that the energy of the DW mode is transferred to the flute mode through the nonlinear interaction.



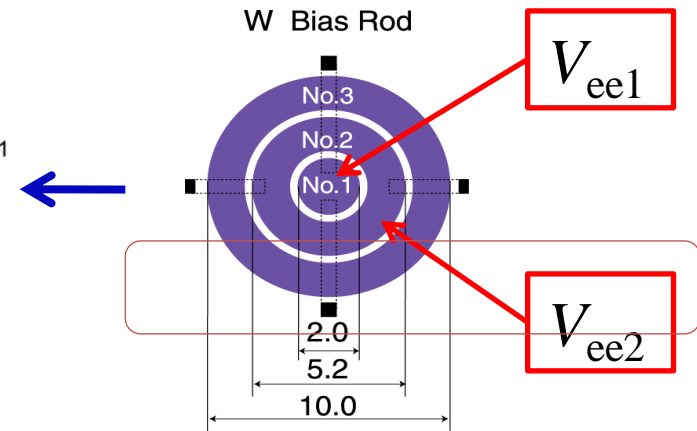
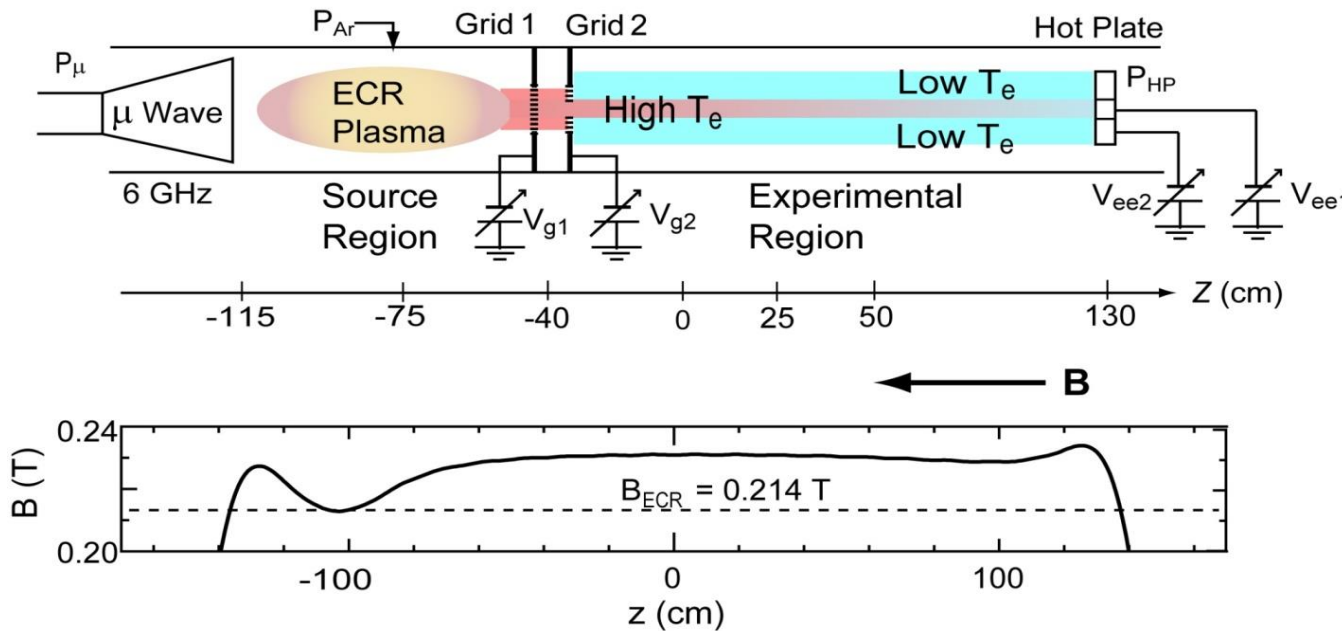
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**Electron emitter
(W hot plate)**

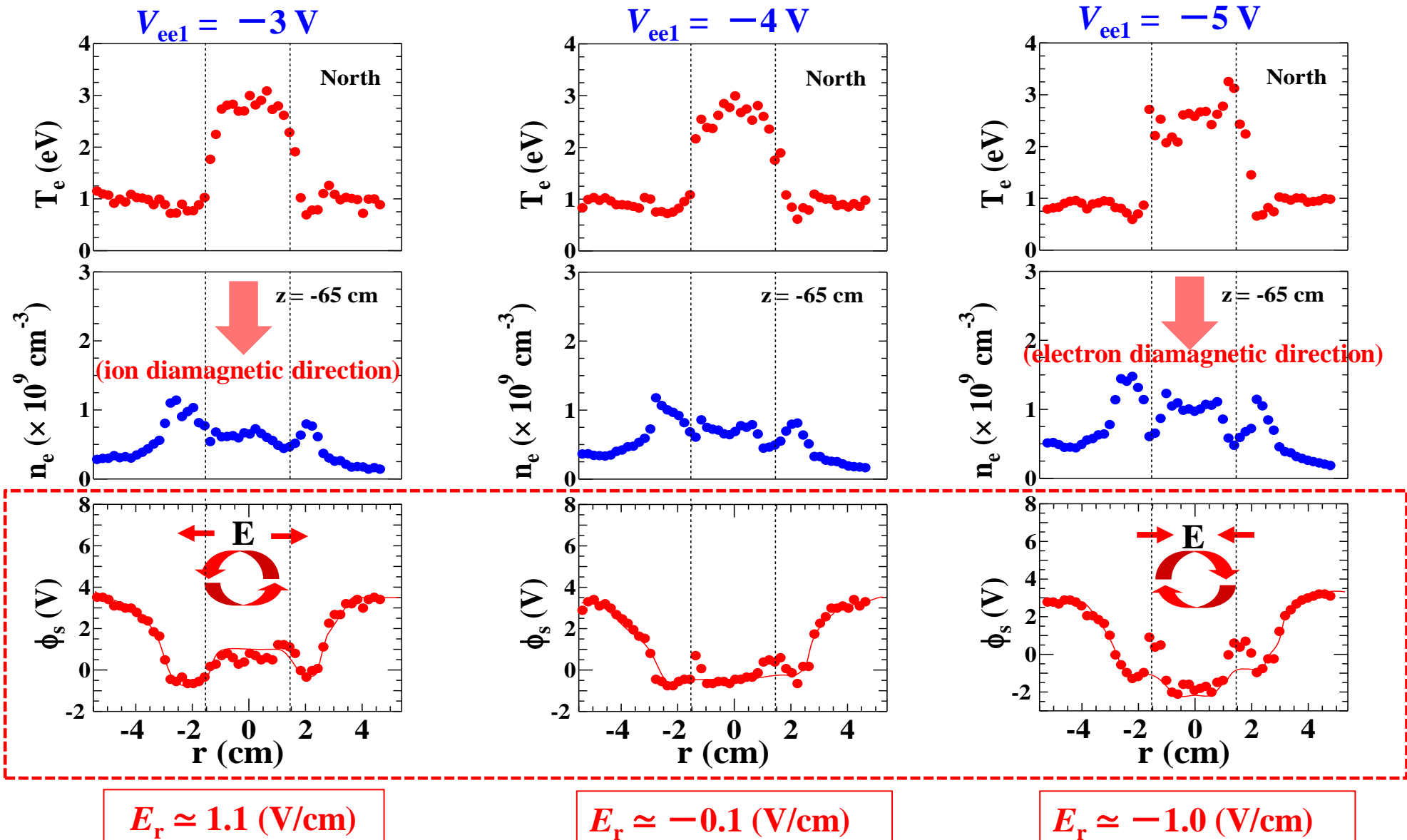
Q_T Upgrade Machine

$$E_r = -\partial\phi(r)/\partial r$$

Control of Radial Electric Field (E_r)

B \otimes

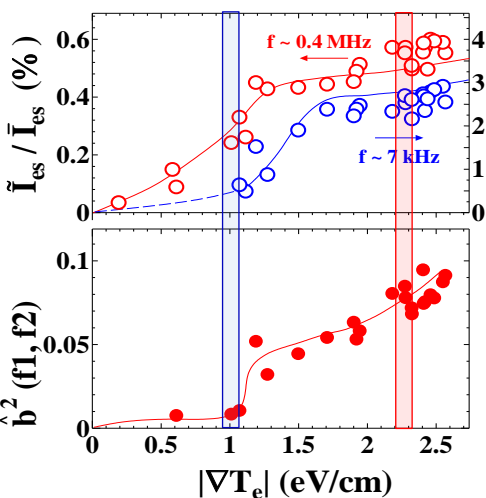
$$P_\mu = 20 \text{ W}, V_{g1} = -10 \text{ V}, V_{g2} = -30 \text{ V}, V_{ee2} = -1.5 \text{ V}$$



Effect of the E_r on Fluctuations

$P_\mu = 20$ W, $V_{g1} = -10$ V,
 $V_{ee2} = -1.5$ V, $r = -0.9$ cm

Nonlinear Coupling
 between ETG mode
 and Drift wave mode

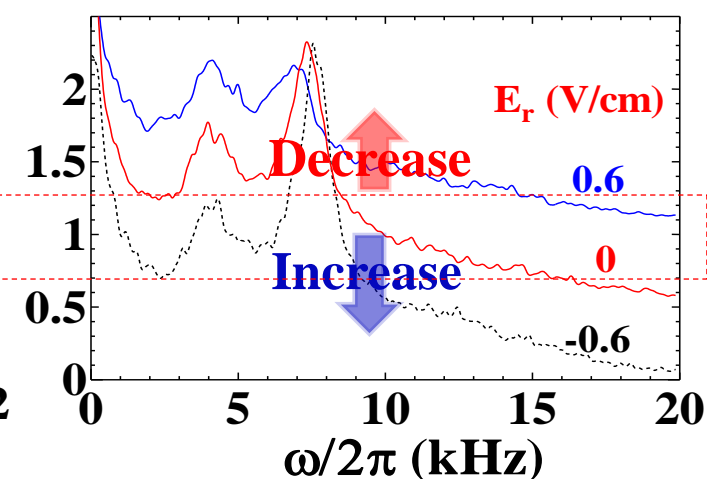
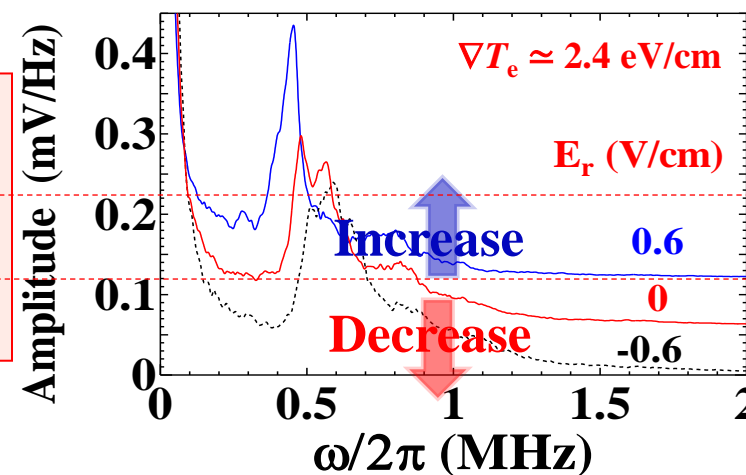
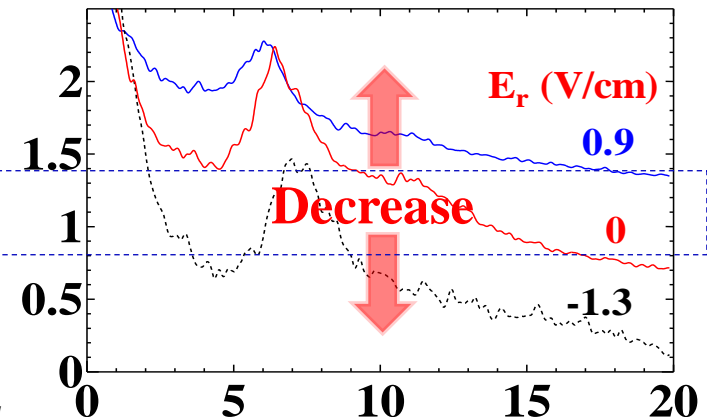
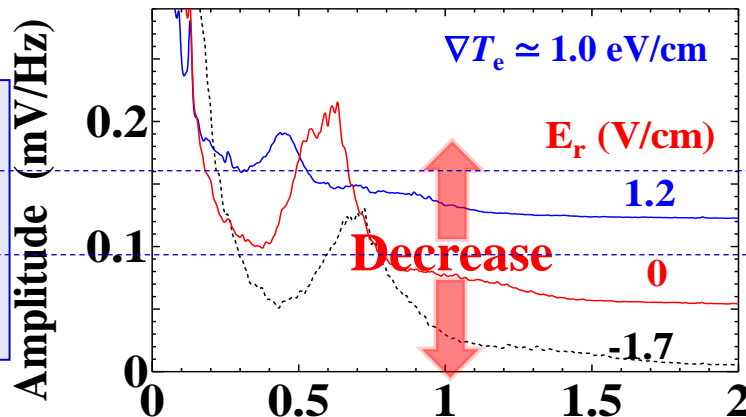


Small ETG

Large ETG

ETG mode

Drift wave mode

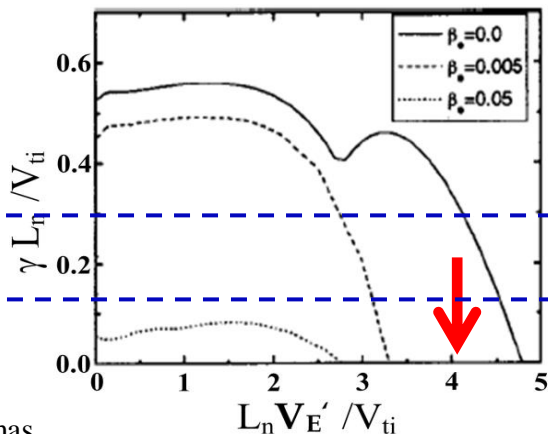


The effect of the E_r on ETG modes in the large ETG case is certainly different from the small ETG case.

Effect of the E_r on Fluctuations

Theories

ETG mode

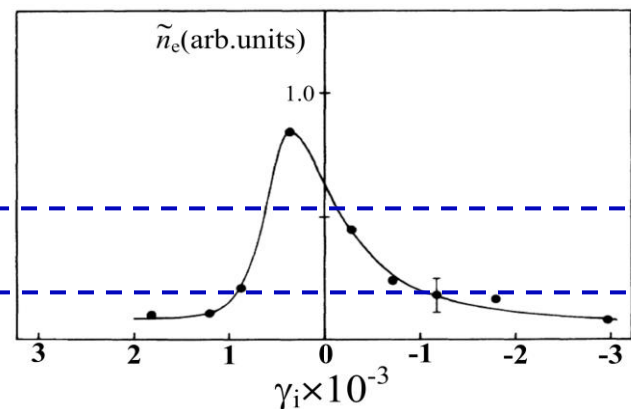


Z. Gao et al., Phys. Plasmas 11, 3053 (2004).

$V_{E'} : \mathbf{E} \times \mathbf{B}$ Shear Strength

Experi.

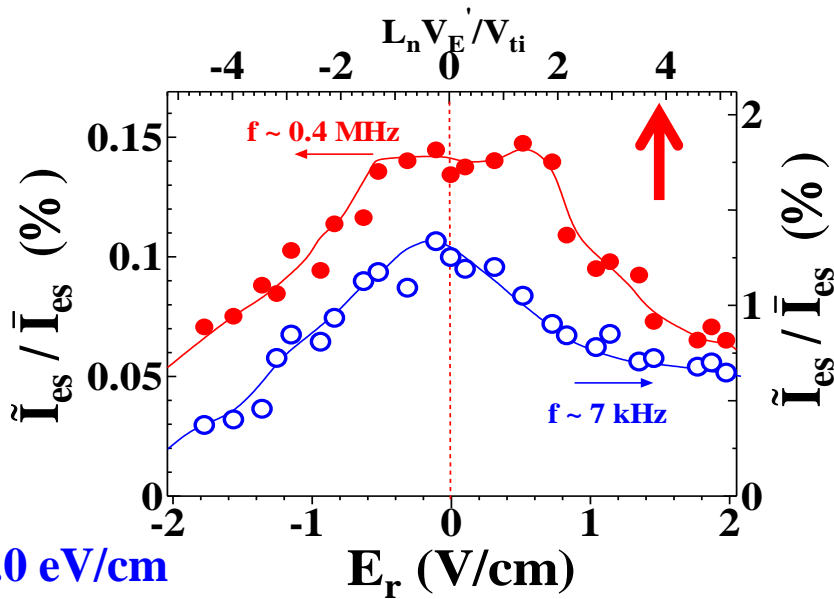
DW mode



A. Mase et al., Phys. Rev. Lett. 64, 2281 (1990).

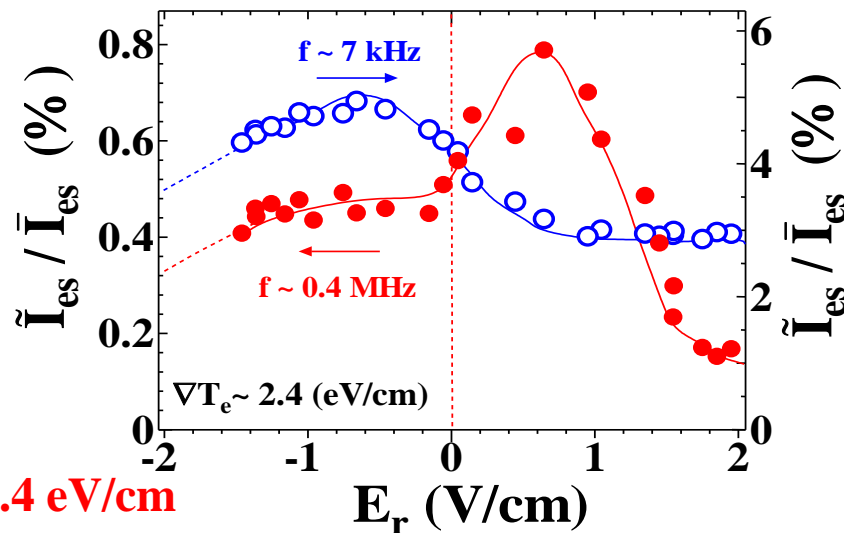
$$\gamma_i \equiv -eE_r / m_i L_\phi \omega_{ce}^2$$

Small ETG



$\nabla T_e \approx 1.0$ eV/cm

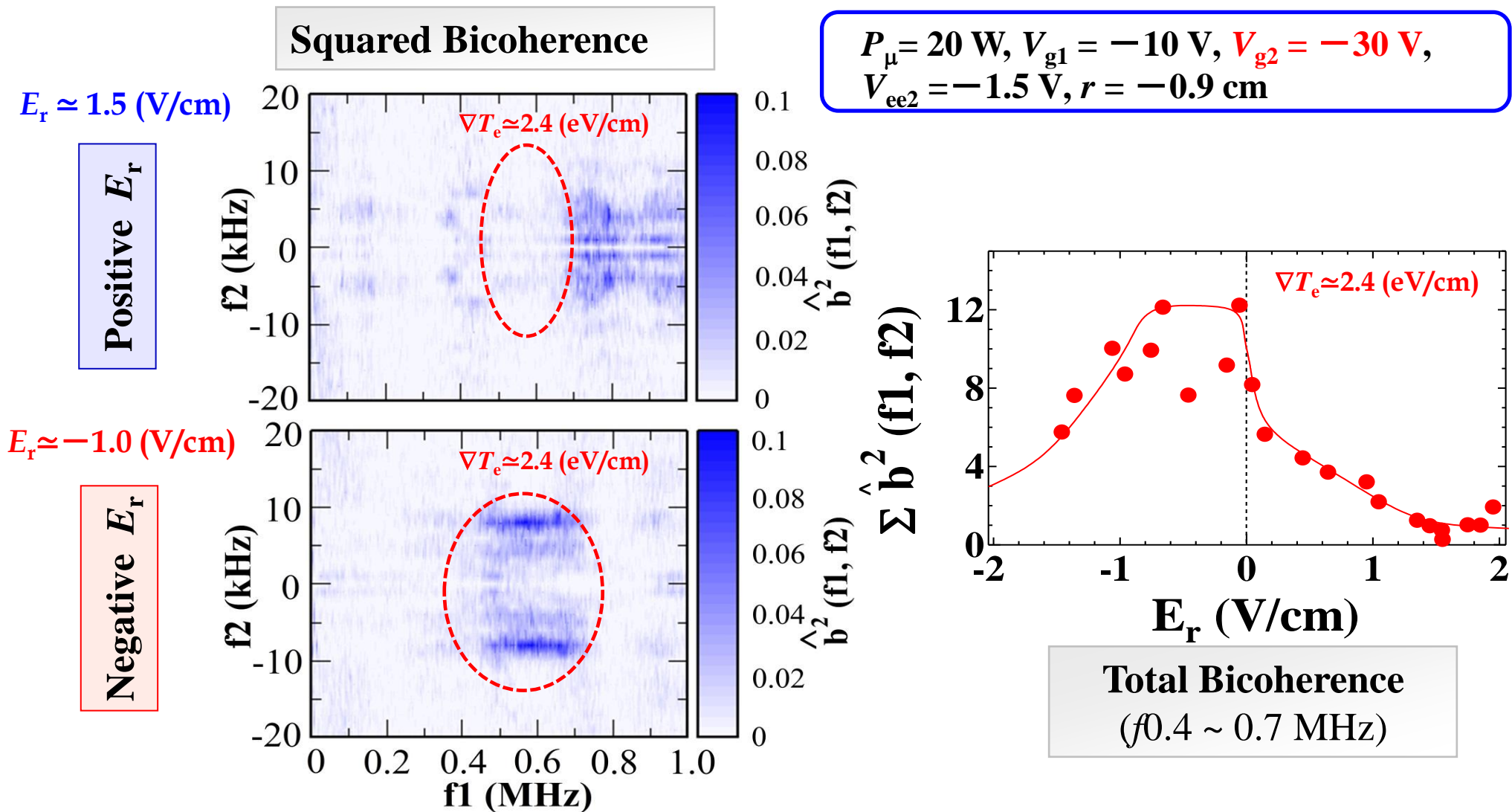
Large ETG



$\nabla T_e \approx 2.4$ eV/cm

The suppression tendency of ETG mode has a significant difference between the slightly negative E_r and positive E_r in the large ETG case.

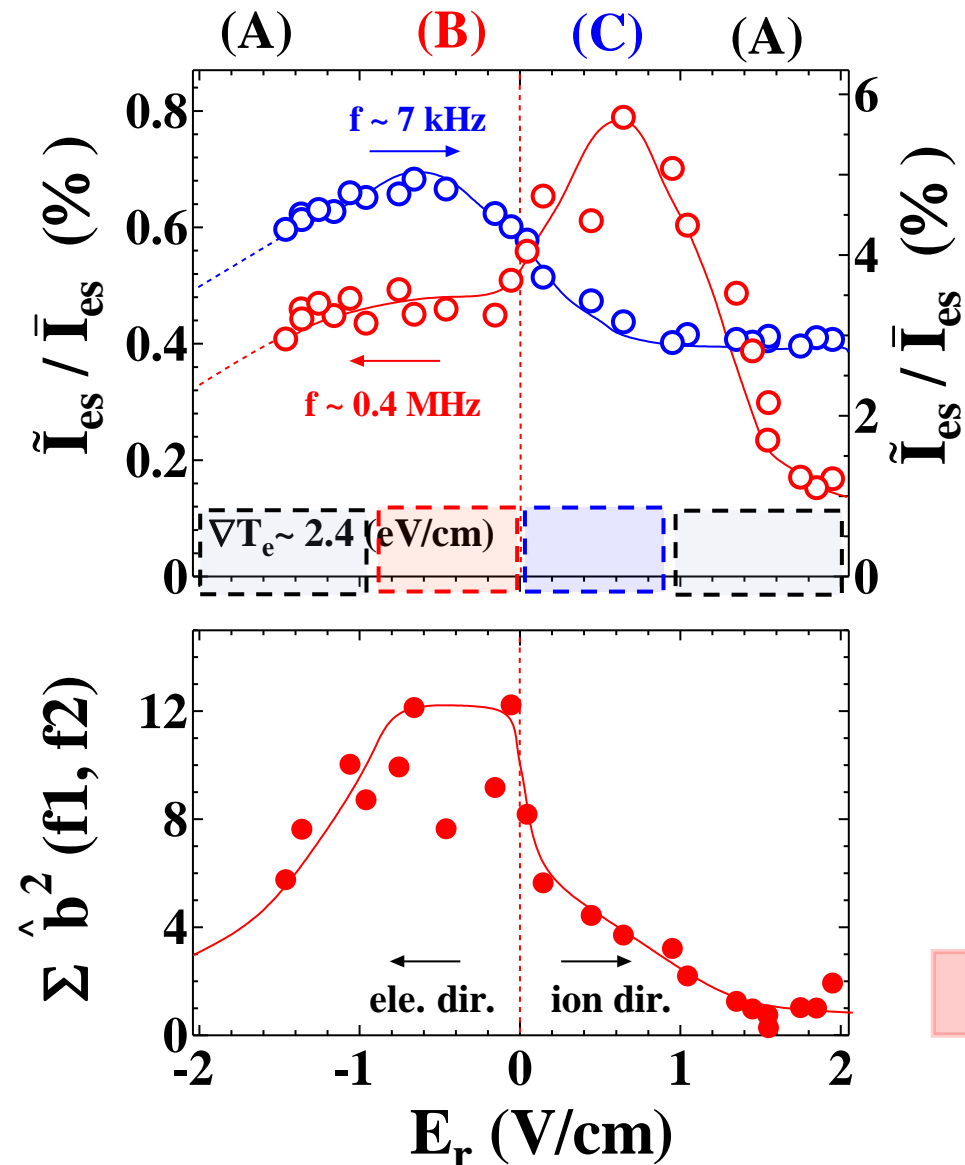
Dependence of bicoherence on the E_r



The nonlinear coupling between the ETG mode and drift wave mode become stronger when E_r becomes the slightly negative value.

Effect of E_r on the Nonlinear Interplay

$$P_\mu = 20 \text{ W}, V_{g1} = -10 \text{ V}, V_{g2} = -30 \text{ V}, V_{ee2} = -1.5 \text{ V}, r = -0.9 \text{ cm}$$



(A) **Suppression of ETG mode**

=> Owing to the strong E_r
Effects of $E \times B$ shear

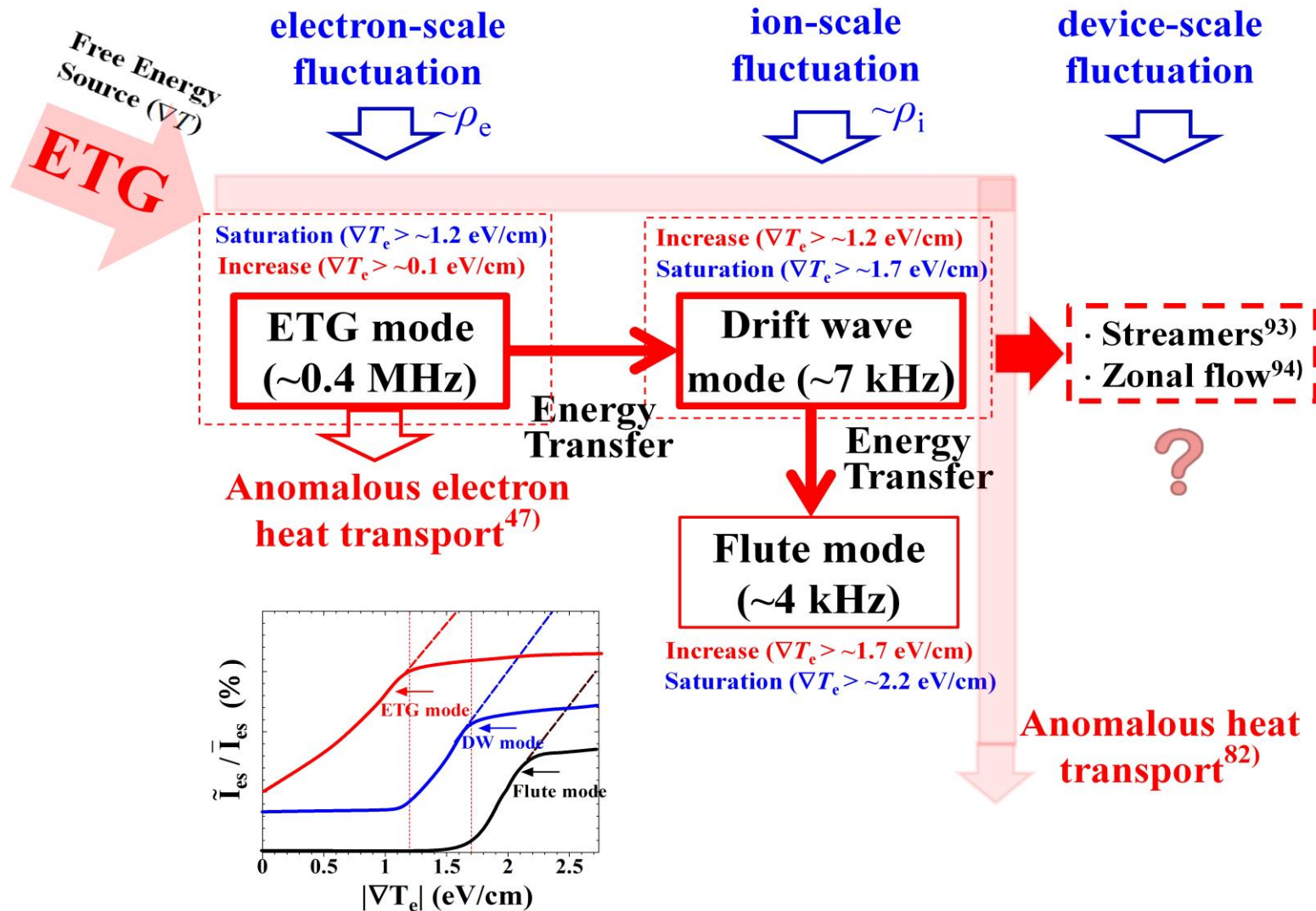
(B) **Suppression of ETG mode**

=> Increasing the Nonlinear Interplay
=> Increasing the DW mode

(C) **Sustainment of ETG mode**

=> Decreasing the Nonlinear Interplay
=> No energy transfer to the DW mode

The E_r affects the nonlinear interaction of the ETG and DW modes, which cause the resultant **suppression of the ETG mode** in the slightly negative E_r .



Refs

- 1) F. ...
- 2) C. Moon, et al., Phys. Rev. Lett. **111**, 115001 (2013).
- 3) Y. Nagashima, et al., Phys. Plasmas **16**, 020706 (2009).
- 4) T. Yamada, et al., Phys. Rev. Lett. **105**, 225002 (2010).